

Supporting Information

Preferential Activation of CO near Hydrocarbon Chains during Fischer-Tropsch Synthesis on Ru

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S1. Details of DFT calculations of thermochemical properties

Frequency calculations were carried out on all optimized states to determine zero-point vibrational energies (*ZPVE*), vibrational enthalpies (H_{vib}), and free energies (G_{vib}). Their values were used, together with VASP-derived electronic energies (E_0), to obtain enthalpies:

$$H = E_0 + ZPVE + H_{vib} + H_{trans} + H_{rot} \quad (S1)$$

and free energies:

$$G = E_0 + ZPVE + G_{vib} + G_{trans} + G_{rot} \quad (S2)$$

for all reactant, product, and transition state structures. For RPBE GGA, the dispersion-corrected enthalpies:

$$H = E_0 + E_d + ZPVE + H_{vib} + H_{trans} + H_{rot} \quad (S3)$$

and free energies:

$$G = E_0 + E_d + ZPVE + G_{vib} + G_{trans} + G_{rot} \quad (S4)$$

Entropy can be determined for a state with a known H and G at a given T :

$$S = \frac{H - G}{T} \quad (S5)$$

For calculations which include the Ru₂₁₈ catalyst model (including adsorbed species and transition states on that surface), there are no translational or rotational degrees of freedom and DFT-derived vibrational frequencies can be used to determine the *ZPVE*, H_{vib} and G_{vib} shown in Eqns. S6-8.

$$ZPVE = \sum_i (1/2 v_i h) \quad (S6)$$

$$H_{vib} = \sum_i \left(\frac{v_i h e^{-\frac{v_i h}{kT}}}{1 - e^{-\frac{v_i h}{kT}}} \right) \quad (S7)$$

$$G_{vib} = \sum_i \left(-kT \ln \frac{1}{1 - e^{-\frac{v_i h}{kT}}} \right) \quad (S8)$$

where v_i is the frequency, h is Planck's constant, k is Boltzmann's constant.

Gas-phase molecules have translational and rotational degrees of freedom; thus H_{trans} , H_{rot} , G_{trans} and G_{rot} must also be computed:¹

$$H_{trans} = \frac{5}{2}kT \quad (\text{S9})$$

$$H_{rot,linear} = kT \quad (\text{S10})$$

$$G_{trans} = -kT \ln \left[\left(\frac{2\pi MkT}{h^2} \right)^{3/2} V \right] \quad (\text{S11})$$

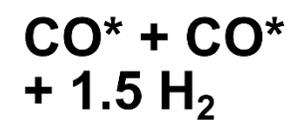
$$G_{rot} = -kT \ln \left[\frac{\pi^{1/2}}{\sigma} \left(\frac{T^3}{\theta_x \theta_y \theta_z} \right)^{1/2} \right] \quad (\text{S12})$$

$$\theta_i = \frac{h^2}{8\pi^2 I_i k} \quad (\text{S13})$$

where I_i is the moment of inertia about axes x, y or z and σ is the symmetry number of the molecule, 2 for H₂, 1 for CO, 2 for H₂O.

¹ Statistical Mechanics”, D. A. McQuarrie, 2000, University Science Books, Sausalito, CA.

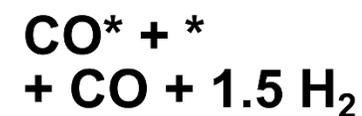
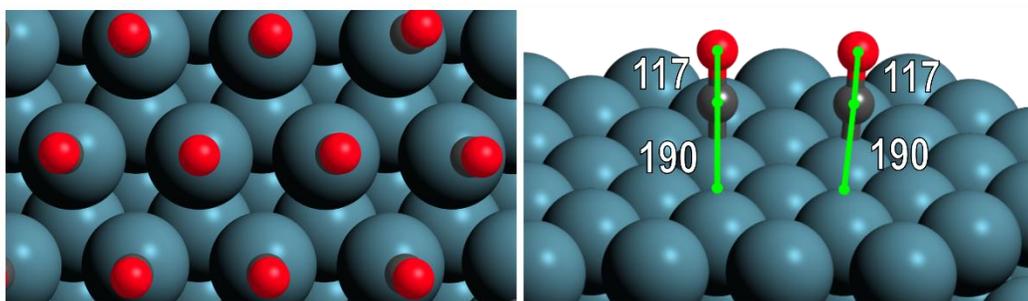
S2. Summary of DFT-derived structures and geometries



$$\Delta H (\text{kJ mol}^{-1}) \quad 0$$

$$\Delta S (\text{J mol}^{-1} \text{K}^{-1}) \quad 0$$

$$\Delta G (\text{kJ mol}^{-1}) \quad 0$$



$$\Delta H (\text{kJ mol}^{-1}) \quad 104$$

$$\Delta S (\text{J mol}^{-1} \text{K}^{-1}) \quad 165$$

$$\Delta G (\text{kJ mol}^{-1}) \quad 22$$

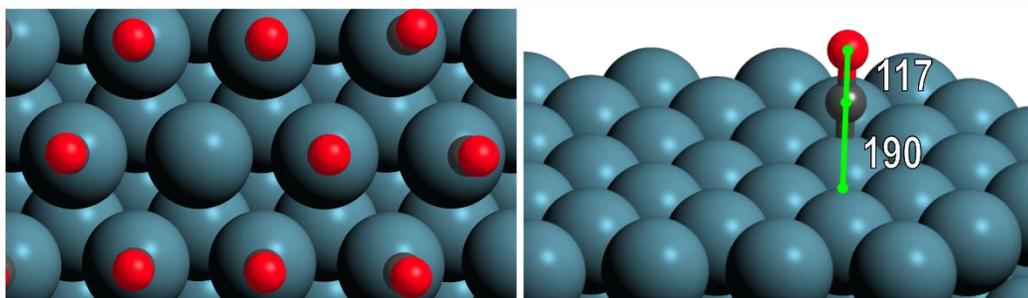


Figure S1. DFT-derived structures (top-down view (left) and side-on view (right) without spectator CO* for clarity) for CO* desorption. The ΔH (kJ mol^{-1}), ΔS ($\text{J mol}^{-1} \text{K}^{-1}$), and ΔG (kJ mol^{-1}) required to form the vacancy from a CO*-covered surface is shown on the left. Other energy-differences shown in Table S1.

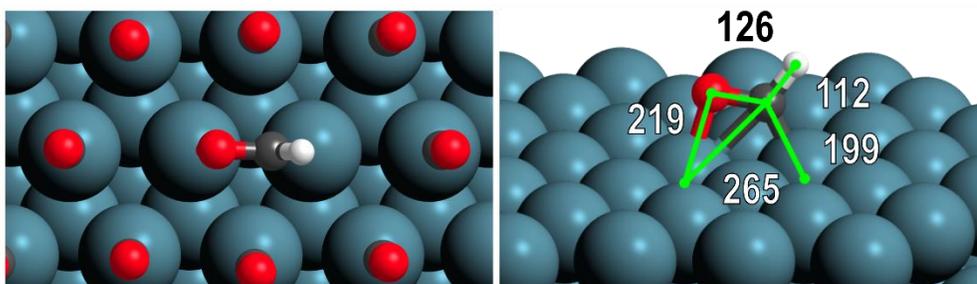
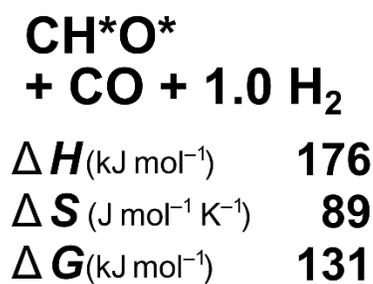
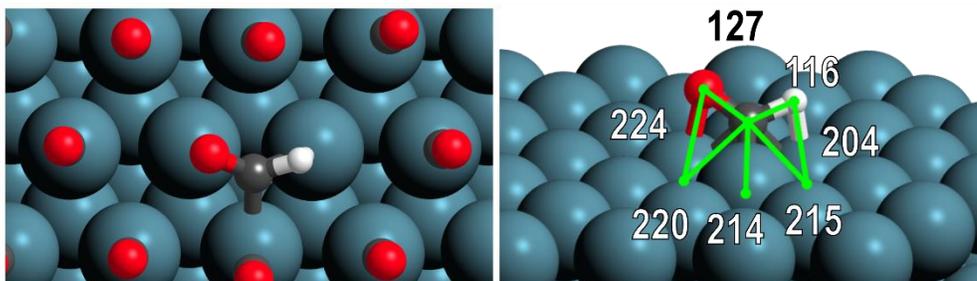
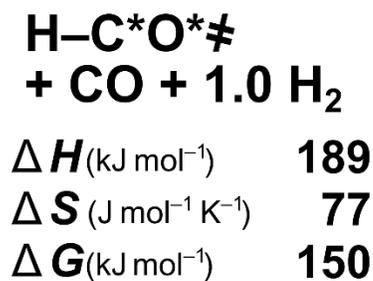
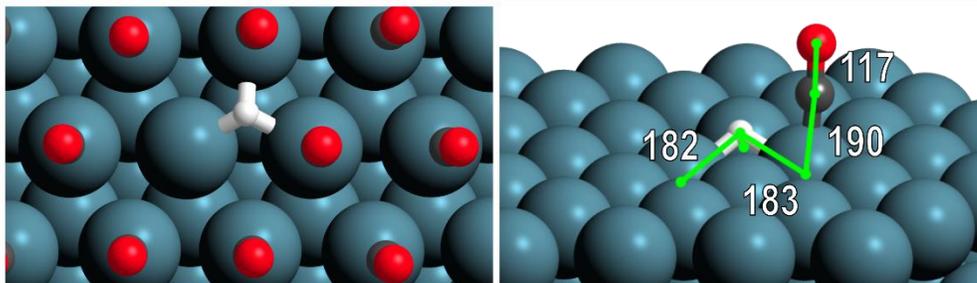
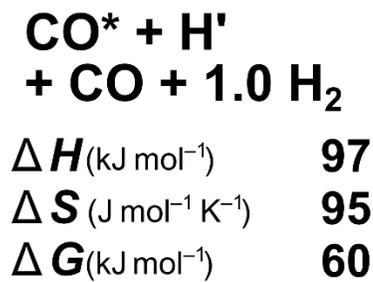


Figure S2. DFT-derived structures (top-down view (left) and side-on view (right) without spectator CO* for clarity) for CH*O* formation. The ΔH (kJ mol⁻¹), ΔS (J mol⁻¹ K⁻¹), and ΔG (kJ mol⁻¹) required to form each state from a CO*-covered surface is shown on the left. Other energy-differences shown in Table S1. Notable bond distances shown in pm.

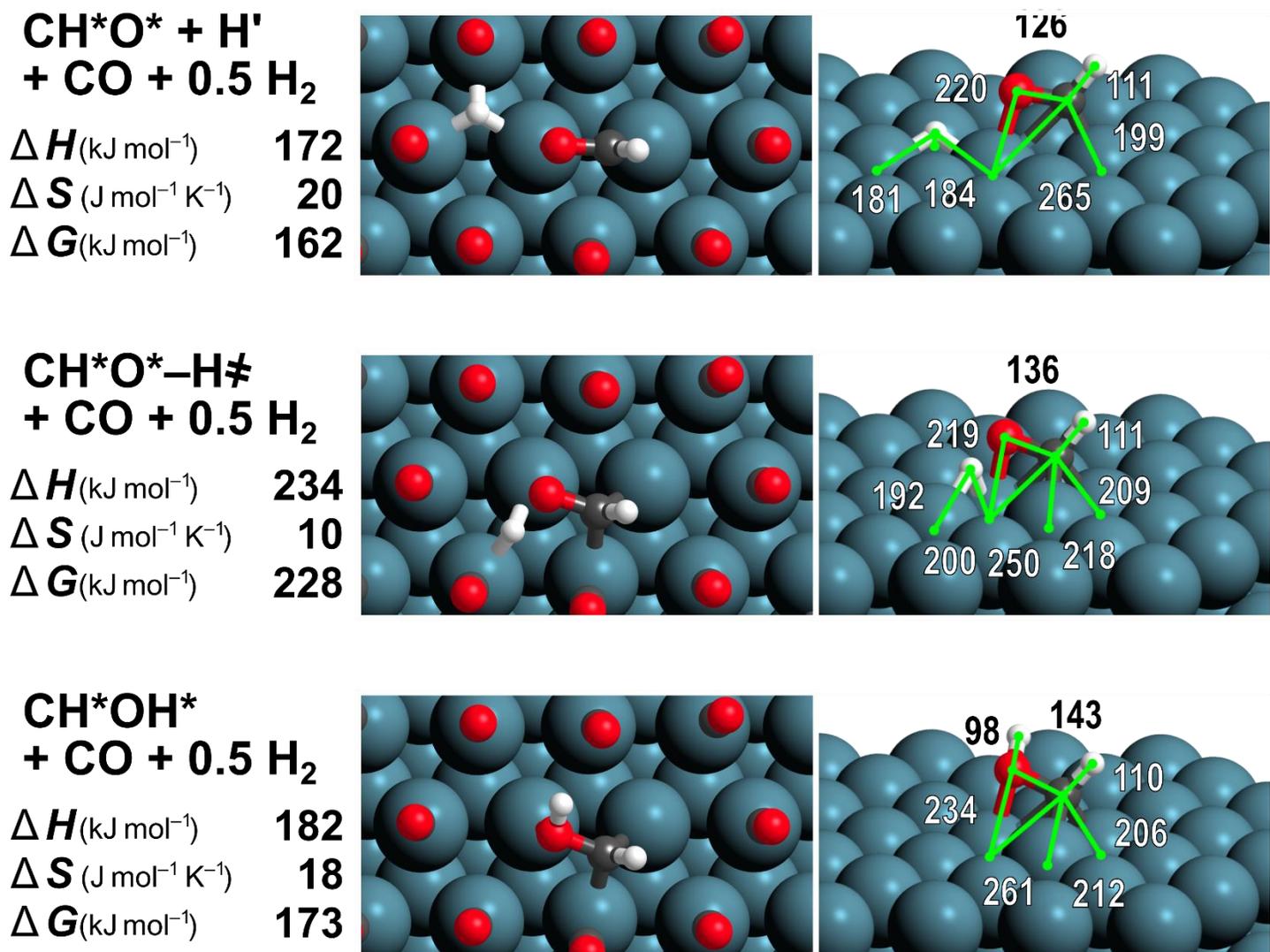


Figure S3. DFT-derived structures (top-down view (left) and side-on view (right) without spectator CO* for clarity) for CH*OH* formation. The ΔH (kJ mol^{-1}), ΔS ($\text{J mol}^{-1} \text{K}^{-1}$), and ΔG (kJ mol^{-1}) required to form each state from a CO*-covered surface is shown on the left. Other energy-differences shown in Table S1. Notable bond distances shown in pm.

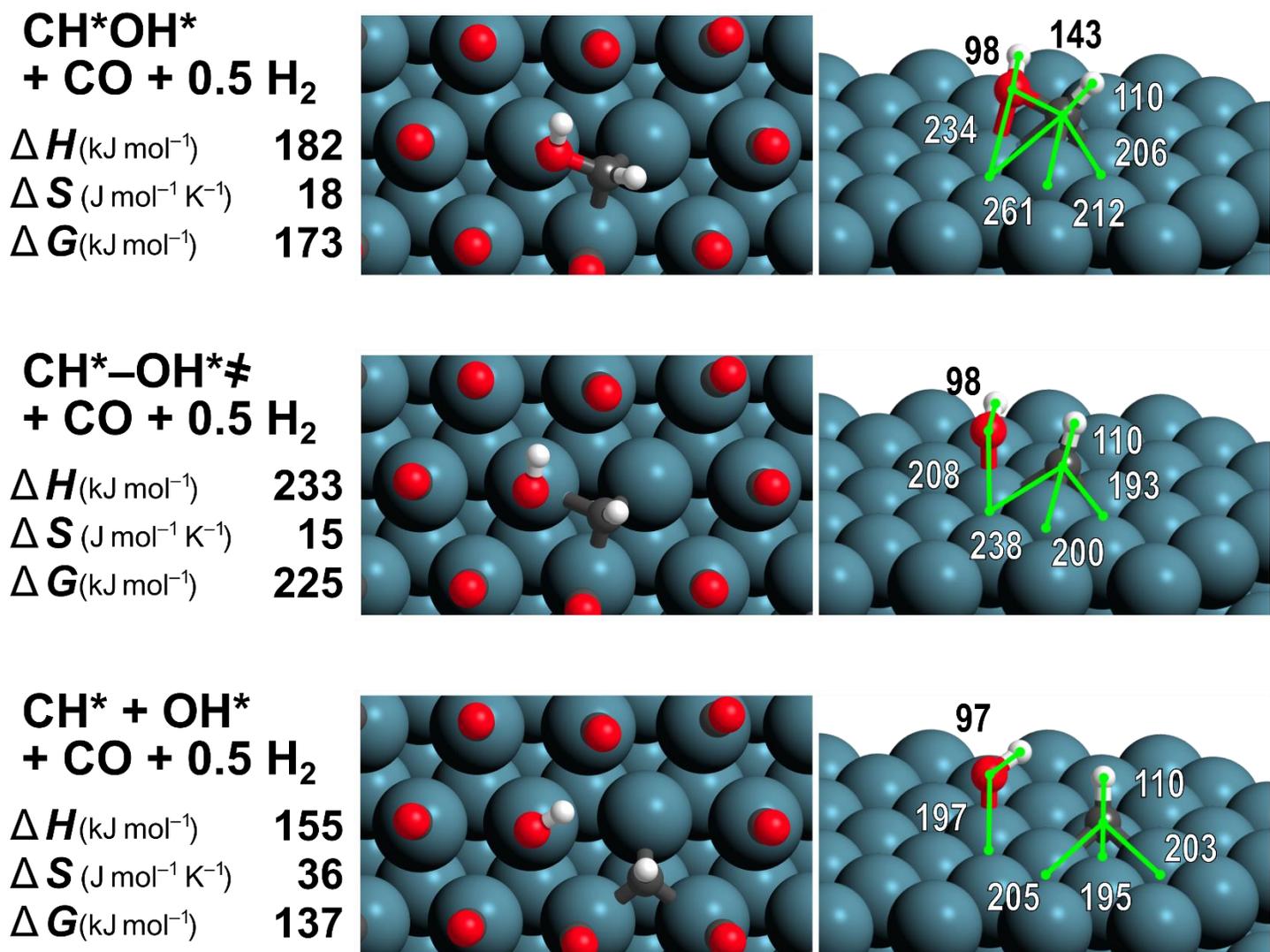


Figure S4. DFT-derived structures (top-down view (left) and side-on view (right) without spectator CO* for clarity) for CH*OH* dissociation. The ΔH (kJ mol⁻¹), ΔS (J mol⁻¹ K⁻¹), and ΔG (kJ mol⁻¹) required to form each state from a CO*-covered surface is shown on the left. Other energy-differences shown in Table S1. Notable bond distances shown in pm.

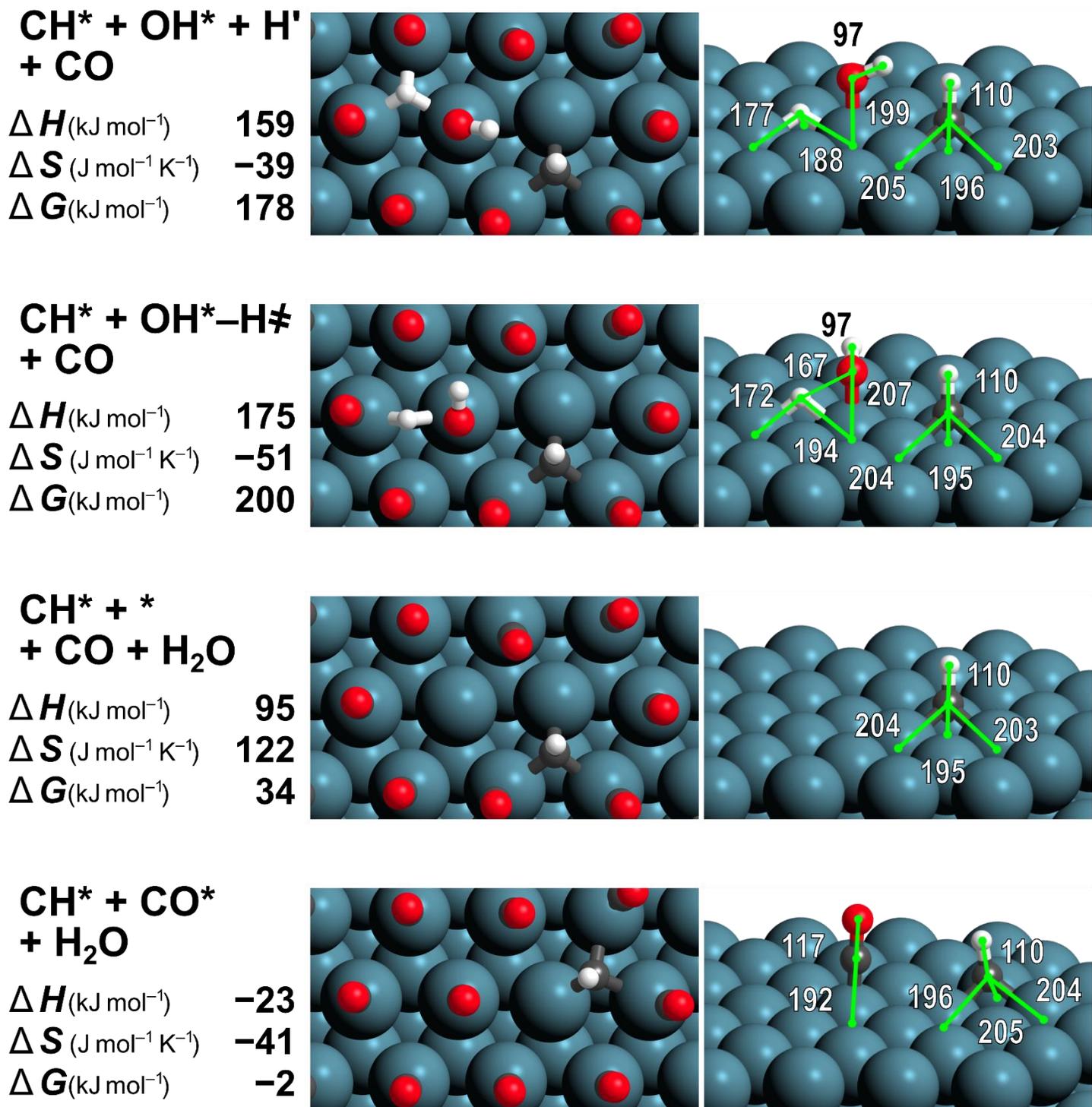


Figure S5. DFT-derived structures (top-down view (left) and side-on view (right) without spectator CO* for clarity) for H₂O formation and CO* re-adsorption. The ΔH (kJ mol⁻¹), ΔS (J mol⁻¹ K⁻¹), and ΔG (kJ mol⁻¹) required to form each state from a CO*-covered surface is shown on the left. Other energy-differences shown in Table S1. Notable bond distances shown in pm.

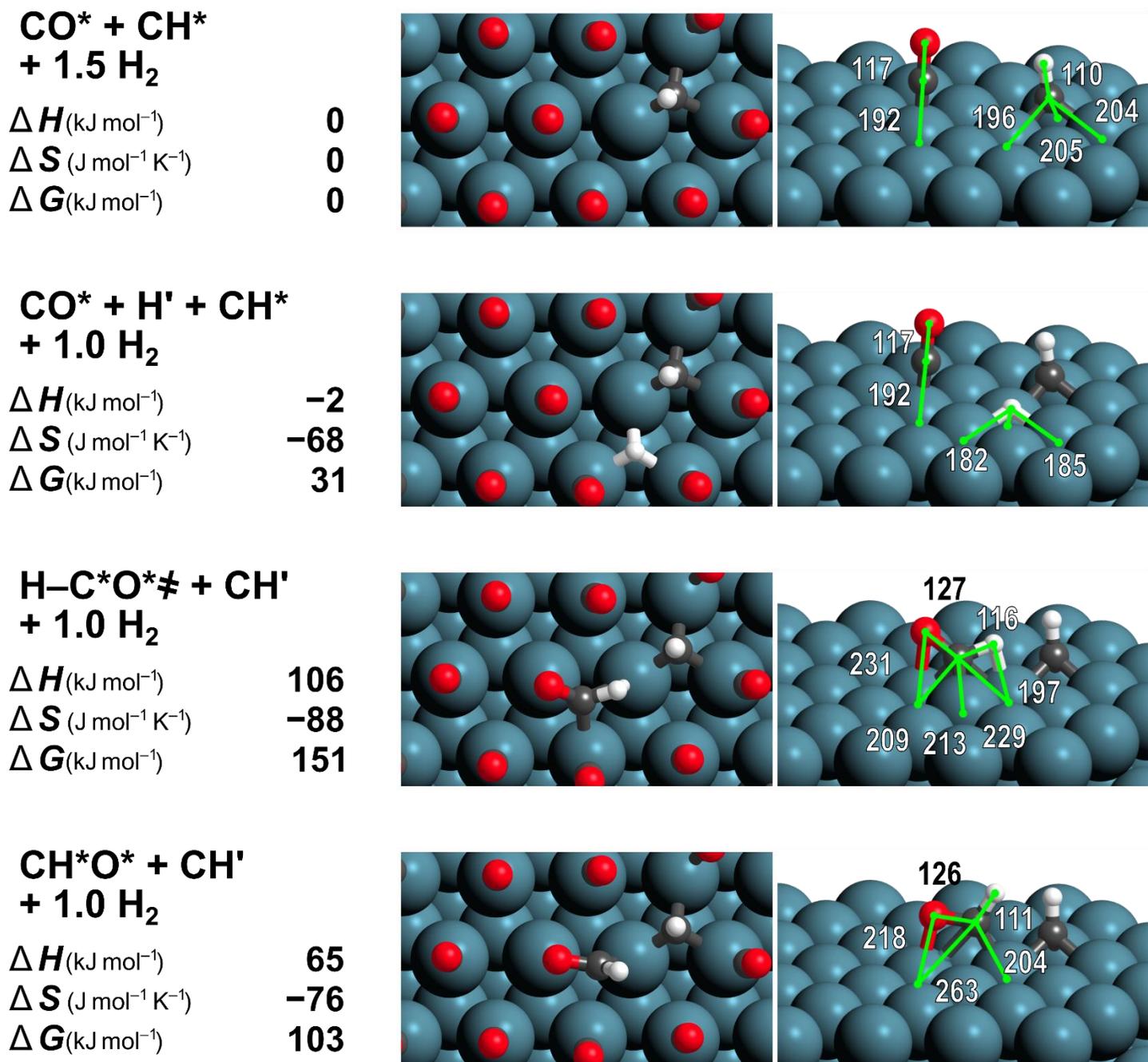
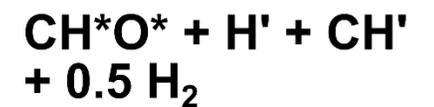


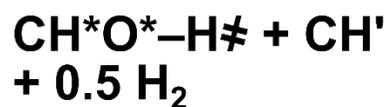
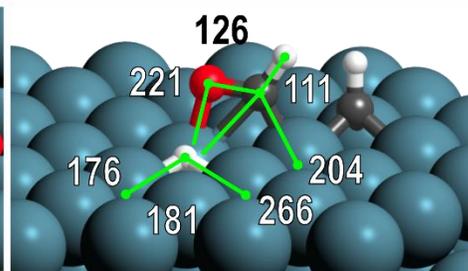
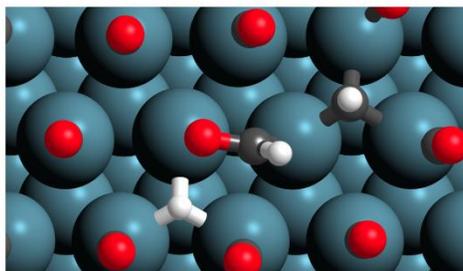
Figure S6. DFT-derived structures (top-down view (left) and side-on view (right) without spectator CO* for clarity) for CH*O* formation vicinal to a CH' chain. The ΔH (kJ mol⁻¹), ΔS (J mol⁻¹ K⁻¹), and ΔG (kJ mol⁻¹) required to form each state from a CO*-covered surface is shown on the left. Other energy-differences shown in Table S2. Notable bond distances shown in pm.



$$\Delta H (\text{kJ mol}^{-1}) \quad 68$$

$$\Delta S (\text{J mol}^{-1} \text{K}^{-1}) \quad -145$$

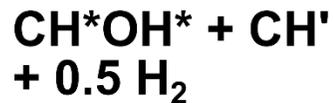
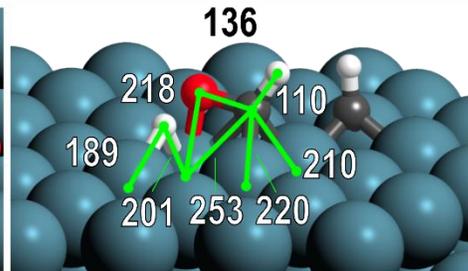
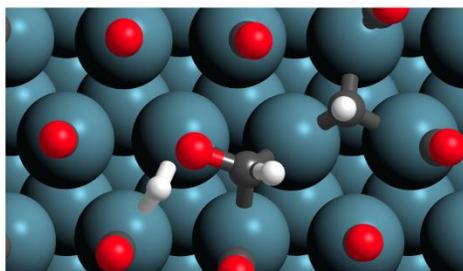
$$\Delta G (\text{kJ mol}^{-1}) \quad 140$$



$$\Delta H (\text{kJ mol}^{-1}) \quad 127$$

$$\Delta S (\text{J mol}^{-1} \text{K}^{-1}) \quad -155$$

$$\Delta G (\text{kJ mol}^{-1}) \quad 204$$



$$\Delta H (\text{kJ mol}^{-1}) \quad 72$$

$$\Delta S (\text{J mol}^{-1} \text{K}^{-1}) \quad -147$$

$$\Delta G (\text{kJ mol}^{-1}) \quad 145$$

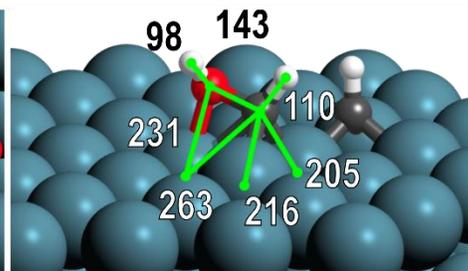
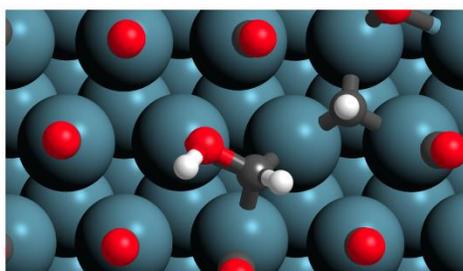


Figure S7. DFT-derived structures (top-down view (left) and side-on view (right) without spectator CO* for clarity) for CH*OH* formation vicinal to a CH' chain. The ΔH (kJ mol^{-1}), ΔS ($\text{J mol}^{-1} \text{K}^{-1}$), and ΔG (kJ mol^{-1}) required to form each state from a CO*-covered surface is shown on the left. Other energy-differences shown in Table S2. Notable bond distances shown in pm.

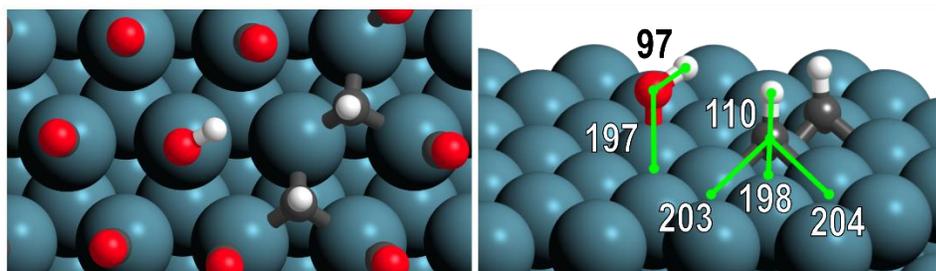
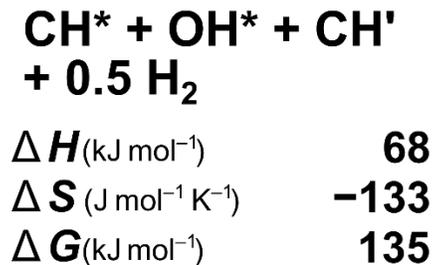
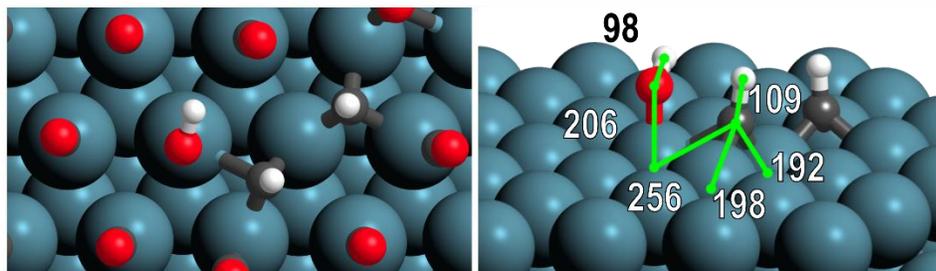
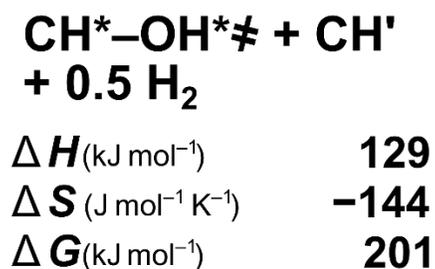
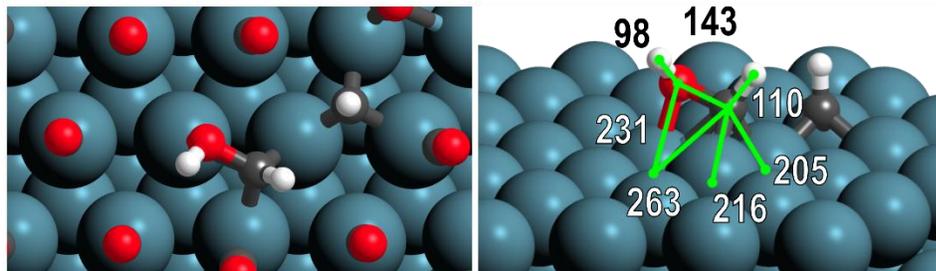
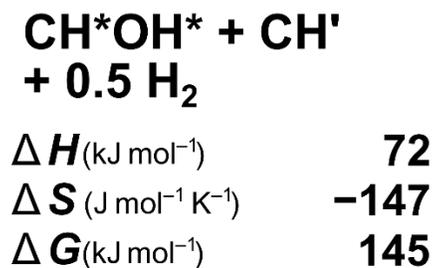


Figure S8. DFT-derived structures (top-down view (left) and side-on view (right) without spectator CO* for clarity) for CH*OH* dissociation vicinal to a CH' chain. The ΔH (kJ mol⁻¹), ΔS (J mol⁻¹ K⁻¹), and ΔG (kJ mol⁻¹) required to form each state from a CO*-covered surface is shown on the left. Other energy-differences shown in Table S2. Notable bond distances shown in pm.

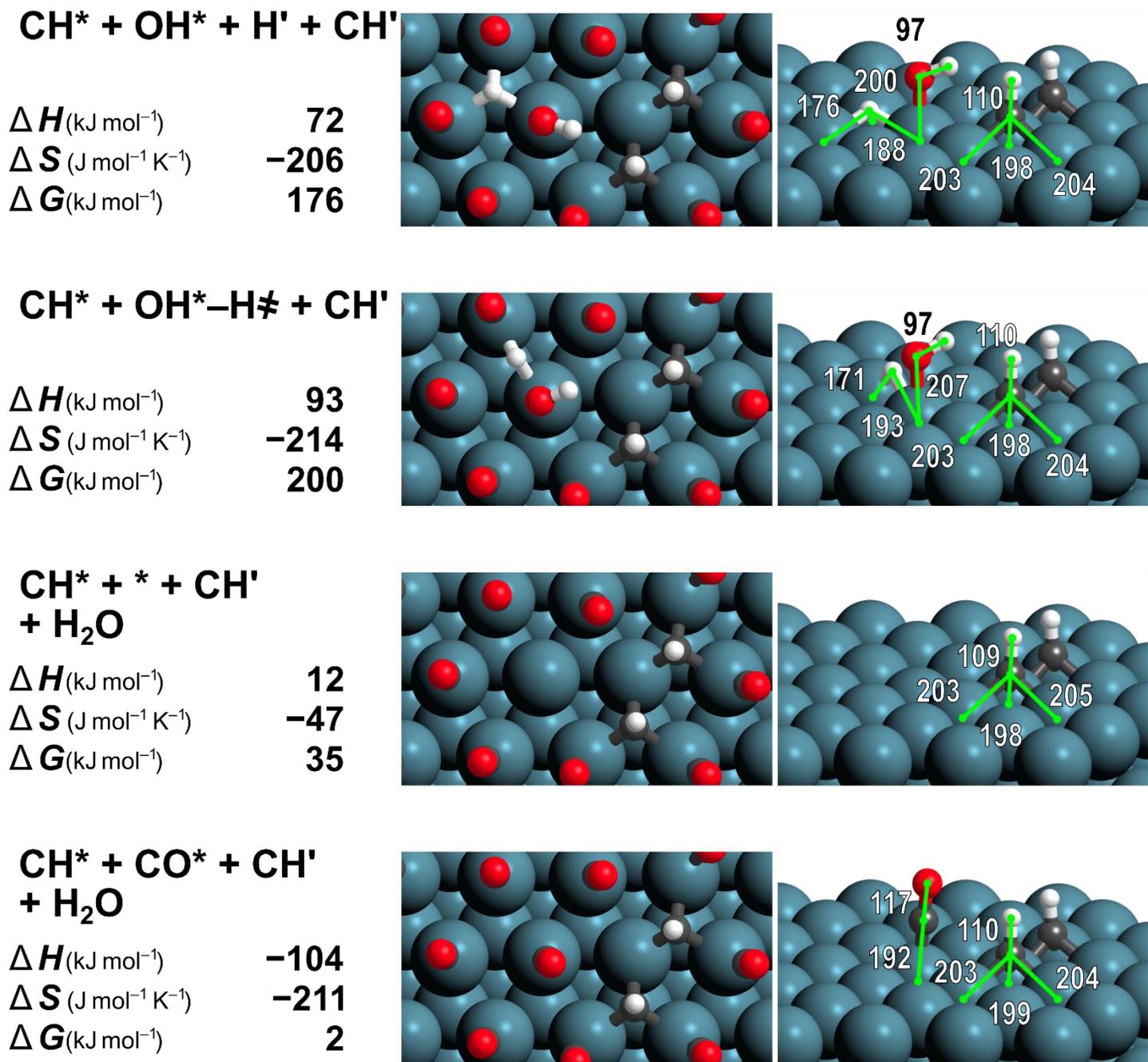


Figure S9. DFT-derived structures (top-down view (left) and side-on view (right) without spectator CO* for clarity) for H₂O formation and CO* re-adsorption vicinal to a CH' chain. The ΔH (kJ mol⁻¹), ΔS (J mol⁻¹ K⁻¹), and ΔG (kJ mol⁻¹) required to form each state from a CO*-covered surface is shown on the left. Other energy-differences shown in Table S2. Notable bond distances shown in pm.

S3. Differences in CO* activation free energies with and without vicinal CH* predicted by different DFT functionals

Table R1. Adsorption free energies for CO* and effective free energy barriers for activating CO* with (ΔG_1^\ddagger) and without (ΔG_0^\ddagger) a vicinal CH*.

		$\Delta G_{\text{ads,CO}}$ kJ mol ⁻¹	ΔG_0^\ddagger kJ mol ⁻¹	ΔG_1^\ddagger kJ mol ⁻¹	$\Delta G_0^\ddagger - \Delta G_1^\ddagger$ kJ mol ⁻¹
RPBE	PAW	+36	199	229	-30
RPBE-D3	PAW	-84	262	196	66
RPBE-D3(NMI)	PAW	-22	228	204	24
PW91	USPP	-18	209	179	30
optB86b-vdW	PAW	-55	224	186	38

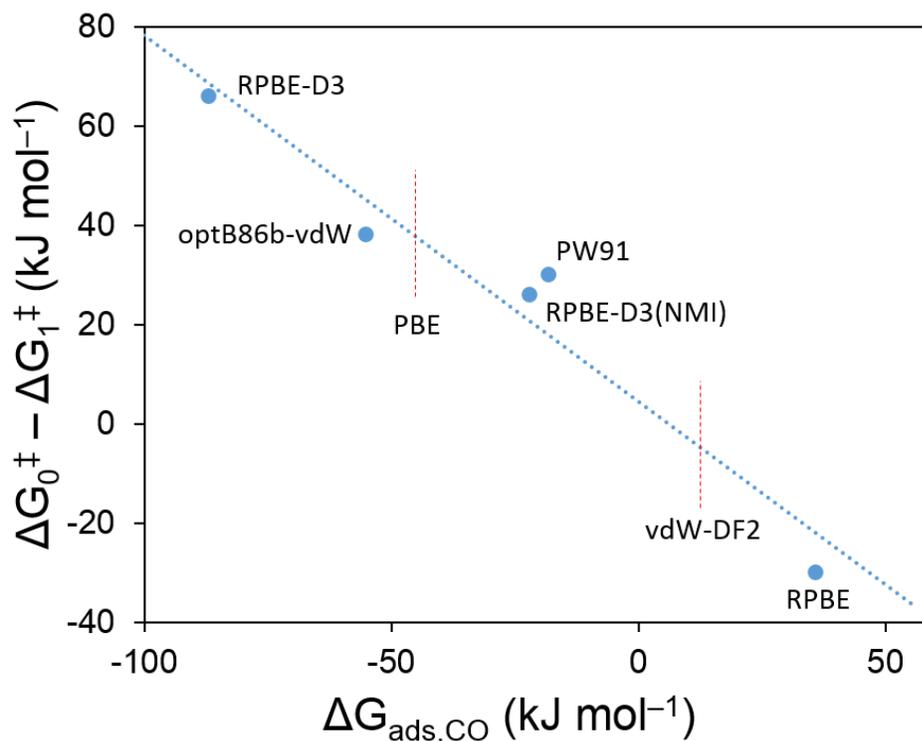


Figure S10. Difference between the effective free energy barrier for CO* activation vicinal to a CH* fragment (ΔG_1^\ddagger) and without a nearby alkylidyne chain (ΔG_0^\ddagger). Vertical dashed lines show the functionals for which the $\Delta G_{\text{ads,CO}}$ was computed but not the free energy barriers for CO* activation.

Effective free energy barriers for CO* activation without a vicinal CH* (ΔG_0^\ddagger) and with a vicinal CH* (ΔG_1^\ddagger) were determined using the RPBE method with PAW and with the D3 method employed for determining dispersive interaction energies between all atoms (RPBE-D3) and only between C, H, and O-atoms (RPBE-D3(NMI)), as reported in the main text. Furthermore, these effective free energy barriers (ΔG_0^\ddagger and ΔG_1^\ddagger) were also computed using the PW-91 method (with USPP) and the optB86b-vdW method (with PAW) which explicitly includes dispersive vdW interactions within the functional. Figure S10 and Table R1 show the correlation between the difference in ‘promoted’ (ΔG_1^\ddagger) and ‘unpromoted’ (ΔG_0^\ddagger) free energy barriers for CO* activation and the adsorption free energy of CO* for all of these methods. Methods which correctly predict negative CO* adsorption free energies (consistent with large CO* coverages during FTS) will also lead to large promotional effects.

S4. Summary of DFT-derived reaction energies

Table S2. Reaction energetics (relative to CO* + CO* state) for H*-assisted CO* dissociation without vicinal chains.

<i>Surface-Bound Species</i>	<i>Gas-Phase Species</i>	ΔE_0	ΔE_{D3}	$\Delta E_{D3,NMI}$	$\Delta ZPVE$	ΔH_{vir}	ΔG_{vir}	ΔH	ΔG	$\Delta H_{D3,NMI}$	$\Delta G_{D3,NMI}$	ΔS
		<i>kJ mol⁻¹</i>										
CO* + CO*	1.5 H ₂	0	0	0	0	0	0	0	0	0	0	0
CO* + *	CO, 1.5 H ₂	53	120	58	-8	-13	11	46	-36	104	22	165
CO* + * + H'	CO, H ₂	61	81	42	-3	-11	11	55	7	97	50	95
H-CO \neq	CO, H ₂	144	97	52	0	-14	17	137	98	189	150	77
HCO**	CO, H ₂	125	86	51	5	-12	14	125	81	176	131	89
HCO + H'	CO, 0.5 H ₂	137	50	33	11	-10	14	138	128	172	162	20
HCO-H \neq	CO, 0.5 H ₂	211	63	29	4	-11	17	204	199	234	228	10
HCOH	CO, 0.5 H ₂	130	88	39	23	-10	15	143	134	182	173	18
HC-OH \neq	CO, 0.5 H ₂	197	76	30	16	-11	15	203	195	233	225	15
CH* + OH*	CO, 0.5 H ₂	114	54	31	17	-7	9	124	106	155	137	36
CH* + OH* + H'	CO	135	14	13	24	-6	11	146	165	159	178	-39
CH* + H-OH* \neq	CO	161	25	10	19	-8	15	165	190	175	200	-51
CH* + *	CO, H ₂ O	15	131	65	25	-19	20	31	-30	95	34	122
CH* + CO*	H ₂ O	-54	20	9	33	-6	9	-32	-11	-23	-2	-41

Table S3. Reaction energetics (relative to CH* + CO* state) for H*-assisted CO* dissociation vicinal to CH*.

<i>Surface-Bound Species</i>	<i>Gas-Phase Species</i>	ΔE_0	ΔE_D	$\Delta E_{D3,NMI}$	$\Delta ZPVE$	ΔH_{vir}	ΔG_{vir}	ΔH	ΔG	$\Delta H_{D3,NMI}$	$\Delta G_{D3,NMI}$	ΔS <i>J mol⁻¹ K⁻¹</i>
CH* + CO*	1.5 H ₂	0	0	0	0	0	0	0	0	0	0	0
CH* + CO* + H'	H ₂	15	-31	-18	5	2	-1	15	49	-2	31	-68
CH' + *H-CO* \neq	H ₂	120	-38	-14	10	-2	6	120	164	106	151	-88
CH' + HCO**	H ₂	74	-39	-17	16	1	2	83	121	65	103	-76
CH' + *HCO* + H'	0.5 H ₂	93	-74	-35	23	2	2	103	176	68	140	-145
CH' + *HCO-H* \neq	0.5 H ₂	162	-53	-36	15	1	6	163	240	127	204	-155
CH' + *HCOH*	0.5 H ₂	79	-47	-29	34	2	3	101	174	72	145	-147
CH' + *HC-OH* \neq	0.5 H ₂	156	-59	-40	25	3	2	169	241	129	201	-144
CH' + CH* + OH*	0.5 H ₂	90	-66	-39	27	5	-1	108	174	68	135	-133
CH' + CH* + OH* + H'	--	109	-99	-56	35	6	0	129	232	72	176	-206
CH' + CH* + H-OH* \neq	--	139	-92	-59	29	5	3	151	258	93	200	-214
CH' + CH* + *	H ₂ O	-4	2	-8	37	-7	10	20	43	12	35	-47
CH' + CH* + CO*	H ₂ O	-71	-114	-63	44	6	-1	-40	65	-104	2	-211

Table S4. Reaction energetics (relative to CH₃C* + CO* state) for H*-assisted CO* dissociation vicinal to CH₃C*.

<i>Surface-Bound Species</i>	<i>Gas-Phase Species</i>	ΔE_0	ΔE_D	$\Delta E_{D3,NMI}$	$\Delta ZPVE$	ΔH_{vir}	ΔG_{vir}	ΔH	ΔG	$\Delta H_{D3,NMI}$	$\Delta G_{D3,NMI}$	ΔS <i>J mol⁻¹ K⁻¹</i>
CH ₃ C* + CO*	1.5 H ₂	0	0	0	0	0	0	0	0	0	0	0
CH ₃ C* + CO* + H'	H ₂	11	-37	-18	5	2	-1	11	44	-7	26	-67
CH ₃ C' + *H-CO* \neq	H ₂	134	-33	-16	10	-2	7	135	180	119	165	-91
CH ₃ C' + HCO**	H ₂	93	-25	-19	17	0	5	102	144	83	125	-84
CH ₃ C' + *HCO* + H'	0.5 H ₂	114	-61	-38	24	1	5	125	201	86	163	-152
CH ₃ C' + *HCO-H* \neq	0.5 H ₂	178	-60	-39	15	1	6	178	257	139	217	-157
CH ₃ C' + *HCOH*	0.5 H ₂	97	-41	-32	35	2	4	118	193	87	162	-150
CH ₃ C' + *HC-OH* \neq	0.5 H ₂	157	-62	-40	25	2	6	169	246	129	206	-154
CH ₃ C' + CH* + OH*	0.5 H ₂	99	-64	-41	27	5	-1	117	183	75	142	-133
CH ₃ C' + CH* + OH* + H'	--	107	-93	-58	34	6	2	124	230	66	172	-211
CH ₃ C' + CH* + H-OH* \neq	--	141	-94	-61	27	5	4	151	260	90	199	-217
CH ₃ C' + CH* + *	H ₂ O	11	-2	-13	37	-8	11	35	60	22	47	-49
CH ₃ C' + CH* + CO*	H ₂ O	-74	-113	-64	43	5	0	-45	63	-109	-1	-215

Table S5. Reaction energetics (relative to C₂H₅C* + CO* state) for H*-assisted CO* dissociation vicinal to C₂H₅C*.

<i>Surface-Bound Species</i>	<i>Gas-Phase Species</i>	ΔE_0	ΔE_D	$\Delta E_{D3,NMI}$	$\Delta ZPVE$	ΔH_{vir}	ΔG_{vir}	ΔH	ΔG	$\Delta H_{D3,NMI}$	$\Delta G_{D3,NMI}$	ΔS <i>J mol⁻¹ K⁻¹</i>
C ₂ H ₅ C* + CO*	1.5 H ₂	0	0	0	0	0	0	0	0	0	0	0
C ₂ H ₅ C* + CO* + H'	H ₂	18	-26	-19	7	1	3	18	56	-1	37	-76
C ₂ H ₅ C' + *H-CO* \neq	H ₂	129	-19	-15	10	-2	7	130	176	115	161	-91
C ₂ H ₅ C' + HCO**	H ₂	92	-18	-19	16	0	5	101	143	82	123	-83
C ₂ H ₅ C' + *HCO* + H'	0.5 H ₂	97	-36	-36	22	2	3	107	180	71	144	-147
C ₂ H ₅ C' + *HCO-H* \neq	0.5 H ₂	172	-51	-38	12	1	7	171	249	133	211	-156
C ₂ H ₅ C' + *HCOH*	0.5 H ₂	81	-56	-31	32	3	4	101	176	70	145	-149
C ₂ H ₅ C' + *HC-OH* \neq	0.5 H ₂	172	-66	-43	25	2	6	185	262	142	219	-155
C ₂ H ₅ C' + CH* + OH*	0.5 H ₂	98	-53	-42	29	3	6	116	191	74	150	-151
C ₂ H ₅ C' + CH* + OH* + H'	--	117	-90	-59	35	5	5	135	245	76	186	-219
C ₂ H ₅ C' + CH* + H-OH* \neq	--	153	-90	-61	29	5	4	165	273	104	212	-216
C ₂ H ₅ C' + CH* + *	H ₂ O	16	11	-13	37	-9	15	39	69	26	56	-60
C ₂ H ₅ C' + CH* + CO*	H ₂ O	-61	-107	-65	45	5	3	-31	80	-96	15	-222

Table S6. Reaction energetics (relative to C₃H₇C* + CO* state) for H*-assisted CO* dissociation vicinal to C₃H₇C*.

<i>Surface-Bound Species</i>	<i>Gas-Phase Species</i>	ΔE_0	ΔE_D	$\Delta E_{D3,NMI}$	$\Delta ZPVE$	ΔH_{vir}	ΔG_{vir}	ΔH	ΔG	$\Delta H_{D3,NMI}$	$\Delta G_{D3,NMI}$	ΔS <i>J mol⁻¹ K⁻¹</i>
C ₃ H ₇ C* + CO*	1.5 H ₂	0	0	0	0	0	0	0	0	0	0	0
C ₃ H ₇ C* + CO* + H'	H ₂	19	-44	-22	6	1	1	19	55	-2	34	-72
C ₃ H ₇ C' + *H-CO* \neq	H ₂	134	-23	-14	10	-1	5	135	177	121	163	-86
C ₃ H ₇ C' + HCO**	H ₂	97	-18	-18	16	4	-8	110	134	92	116	-48
C ₃ H ₇ C' + *HCO* + H'	0.5 H ₂	98	-38	-37	22	2	1	108	180	71	143	-144
C ₃ H ₇ C' + *HCO-H* \neq	0.5 H ₂	183	-56	-39	14	1	4	183	258	145	220	-150
C ₃ H ₇ C' + *HCOH*	0.5 H ₂	85	-55	-30	31	3	2	105	177	74	147	-144
C ₃ H ₇ C' + *HC-OH* \neq	0.5 H ₂	175	-61	-44	25	6	-3	192	256	148	212	-128
C ₃ H ₇ C' + CH* + OH*	0.5 H ₂	99	-60	-42	28	3	4	116	189	74	147	-147
C ₃ H ₇ C' + CH* + OH* + H'	--	117	-92	-59	35	5	5	136	244	76	185	-218
C ₃ H ₇ C' + CH* + H-OH* \neq	--	155	-82	-62	28	8	-4	170	267	108	205	-194
C ₃ H ₇ C' + CH* + *	H ₂ O	18	13	-12	36	-8	14	40	69	28	56	-57
C ₃ H ₇ C' + CH* + CO*	H ₂ O	-59	-106	-65	45	5	2	-29	80	-95	15	-219

S5. Derivation of modified CO consumption rate equation

The total CO* consumption expression, including the vicinal CO-activation mechanism, is derived here based on Langmuir-Hinshelwood kinetics. In Scheme 1, CO* is consumed in the irreversible addition of the second H' to form the CH*OH* transition state, which can occur either next to a growing chain or in an unperturbed CO*-covered surface. The total CO* consumption rate in this process represents the sum of consumption near each length growing chain, which can be written as:

$$r_{CO} = k_{CHOH,0}K_{CHO,0}[CO^*][*][H']^2 + \sum_i(k_{CHOH,i}K_{CHO,i}[CO^*][C_i^*][H']^2) \quad (S14)$$

where r_{CO} is the net rate of CO consumption, $k_{CHOH,0}$ is the CH*OH* formation activation rate constant with no growing chains nearby, $k_{CHOH,i}$ is the CH*OH* formation activation rate constant vicinal to a chain of length i , $[CO^*]$ represents CO surface concentration, $[*]$ represents vacant site surface concentration, and $[H']$ represents hydrogen surface coverage in *non-competitive adsorption* with carbon-based adsorbates.

By assuming that hydrogen undergoes non-competitive adsorption, the concentration of surface hydrogen can be related to the gas phase pressure by:

$$[H'] = [K_{H_2}(H_2)]^{0.5} \quad (S15)$$

Assuming that CO* is the most abundant surface intermediate, and that CO* is quasi-equilibrated with the gas phase, the surface concentration of CO* and free sites * can be represented as:

$$[CO^*] = \frac{K_{CO}(CO)}{1+K_{CO}(CO)} \quad (S16)$$

$$[*] = \frac{1}{1+K_{CO}(CO)} \quad (S17)$$

Using an Anderson-Shulz-flory formalism, the concentration of any length growing chain can be related back to the concentration of C₁ chains and the chain growth probability using:

$$[C_n^*] = [C_1^*] \prod_{i=1}^n \alpha_{i-1} \quad (S18)$$

where the chain growth probability is defined as the rate of propagation of a growing chain:

$$\alpha_i = \frac{r_{growth,i}}{r_{growth,i} + r_{term,i}} \quad (S19)$$

and the rate constants governing CO-activation can be condensed into γ using:

$$\gamma_n = k_{HCOH,n}K_{HCO}K_{H_2} \quad (S20)$$

By combining equations S14-S20, the net consumption of CO can be expressed as:

$$r_{CO} = \frac{\gamma_0 K_{CO}(CO)(H_2)}{[1+K_{CO}(CO)]^2} + \frac{K_{CO}(CO)(H_2)[C_1^*] \sum_{n=1}^{\infty} \gamma_n \prod_{i=1}^n \alpha_{i-1}}{1+K_{CO}(CO)} \quad (S21)$$

The only surface concentration term in this equation is the concentration of C_1 growing chains. This quantity can be determined by employing the pseudo-steady-state-hypothesis on C_1 chains, where the net rate of generation can be expressed as:

$$r_{C_1} = 0 = \frac{\gamma_0 K_{CO}(CO)(H_2)}{[1+K_{CO}(CO)]^2} - k_{methane}[C_1^*][K_{H_2}(H_2)]^{1.5} - \frac{\gamma_1 K_{CO}(CO)(H_2)[C_1^*]}{1+K_{CO}(CO)} \quad (S22)$$

The term reflecting the consumption due to methane can be eliminated by substituting the chain growth parameter for C_1 chains, α_1 , using:

$$\alpha_1 = \frac{\frac{\gamma_1 K_{CO}(CO)(H_2)[C_1^*]}{1+K_{CO}(CO)}}{\frac{\gamma_1 K_{CO}(CO)(H_2)[C_1^*]}{1+K_{CO}(CO)} + k_{methane}[C_1^*][K_{H_2}(H_2)]^{1.5}} \quad (S23)$$

By combining equation S22 and S23, the concentration of growing chains can be related to the concentration of vacant surface sites at steady state:

$$[C_1^*] = \frac{\gamma_0 [C_1^*] \alpha_1}{\gamma_1} = \frac{\gamma_0 \alpha_1}{\gamma_1 [1+K_{CO}(CO)]} \quad (S24)$$

Combining the result of equation S24 with the CO consumption equation in S21 yields:

$$r_{CO} = \frac{\gamma_0 K_{CO}(CO)(H_2)}{[1+K_{CO}(CO)]^2} + \frac{\gamma_0 \alpha_1 K_{CO}(CO)(H_2) \sum_{n=1}^{\infty} \gamma_n \prod_{i=1}^n \alpha_{i-1}}{\gamma_1 [1+K_{CO}(CO)]^2} \quad (S25)$$

which can be rearranged to yield the final expression:

$$r_{CO} = \frac{\gamma_0 K_{CO}(CO)(H_2)}{[1+K_{CO}(CO)]^2} \left(1 + \alpha_1 \sum_{n=1}^{\infty} \left(\frac{\gamma_n}{\gamma_1} \right) \prod_{i=1}^n \alpha_{i-1} \right) \quad (S26)$$