

## **Supporting Information**

### **Mechanism and Kinetics of Methylating C<sub>6</sub>–C<sub>12</sub> Methylbenzenes with Methanol and Dimethyl Ether in H-MFI Zeolites**

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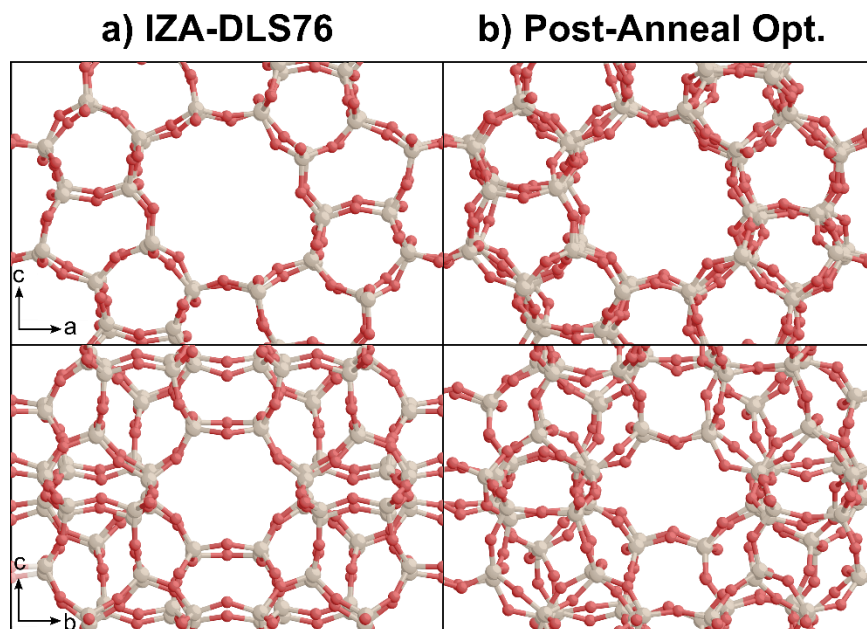
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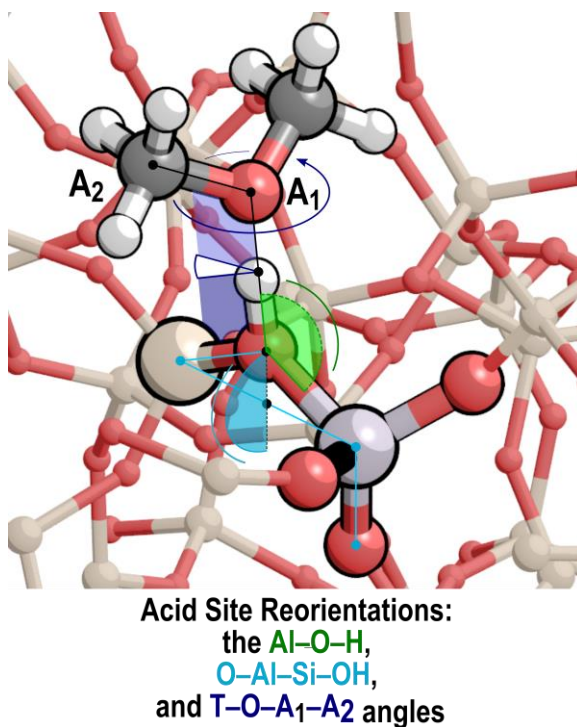
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*S1. Details of MFI Restructuring and Reorientations*

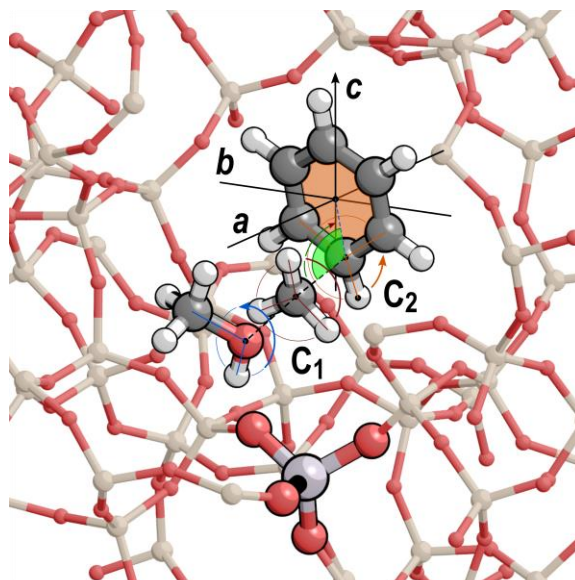


**Figure S1.** **a)** The initial, unoptimized silica form of MFI from the IZA database (IZA-DLS76) and **b)** the structure obtained after annealing and optimization using PBE-D. The post-anneal structure is  $23 \text{ kJ mol}^{-1}$  more stable than the directly optimized IZA-DLS76 structure.



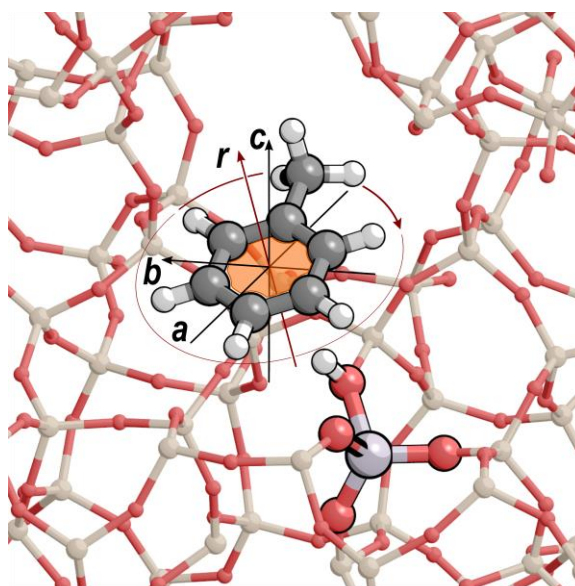
**Figure S2.** Three different acid site reorientations resulting from altering the  $\text{Al-O}_a\text{-A}_1$  angle (green),  $\text{O}_t\text{-Al-Si-O}_a$  angle (cyan), and  $\text{O}_t\text{-O}_a\text{-A}_1\text{-A}_2$  angle (blue).





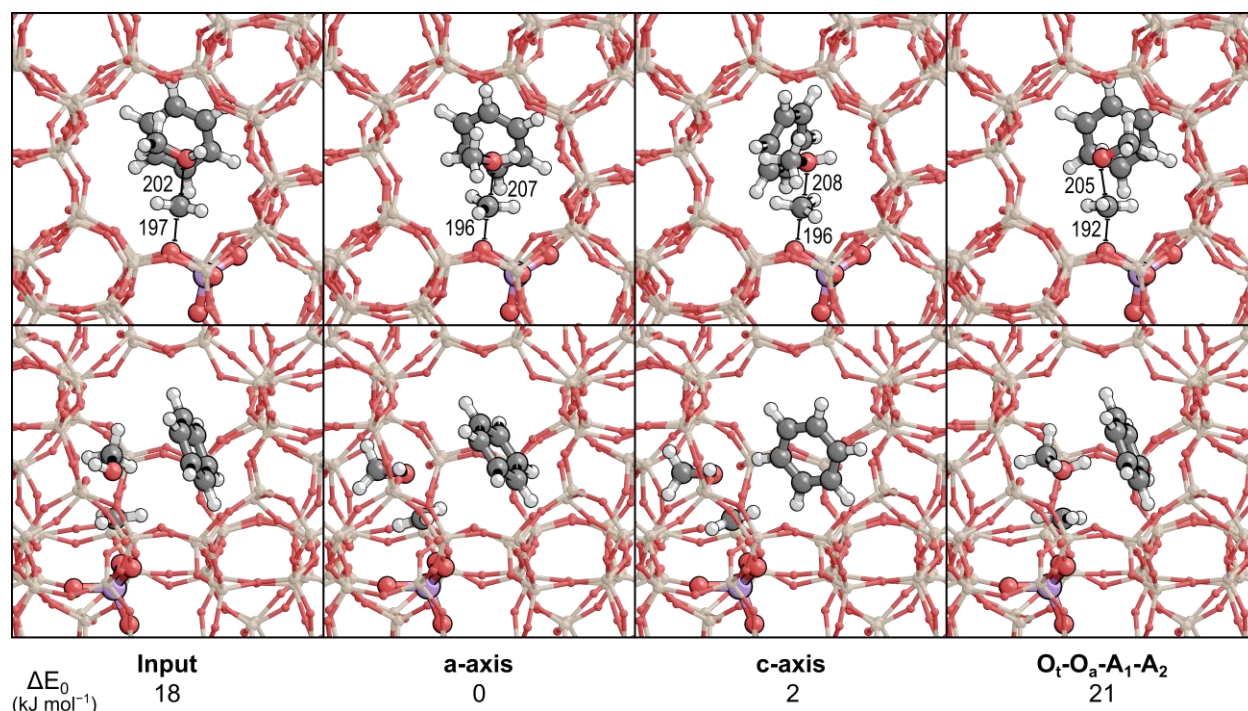
**Internal Reorientations:**  
 $\text{CH}_3\text{OH}$ ,  $\text{CH}_3$ , and  $\text{C}_6\text{H}_6$   
 around the  $\text{O}-\text{C}_1-\text{C}_2$  axes;  
 and the  $\text{CH}_3$ -ring angle.

**Figure S3.** Internal reorientations of the concerted transition state where  $\text{CH}_3\text{OH}$  (blue),  $\text{CH}_3$  (brown), and  $\text{C}_6\text{H}_6$  can be rotated by altering the  $\text{O}_m-\text{C}_1-\text{C}_2$  angle formed between the leaving group, the adding  $\text{CH}_3$ , and the ring (orange). The angle of the ring can be altered relative to the adding  $\text{CH}_3$  group by altering the  $\text{CH}_3$ -ring angle (green).

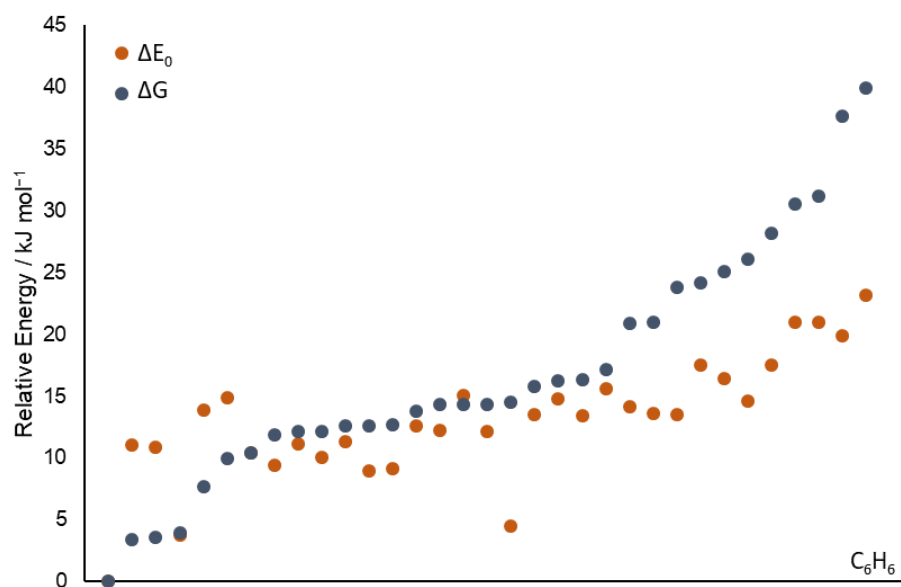


**Spatial Reorientations:**  
 around the  $a$ ,  $b$ , and  $c$   
 vectors, and the axis  
 perpendicular to the ring ( $r$ ).

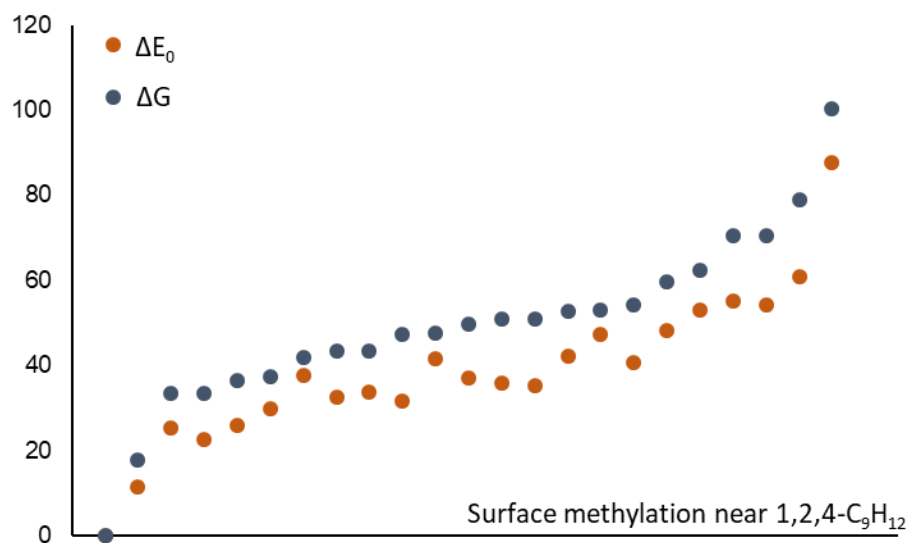
**Figure S4.** Spatial reorientations of toluene about the  $a$ ,  $b$ , and  $c$  axes of the unit cell and the axis perpendicular to the center of the ring (red).



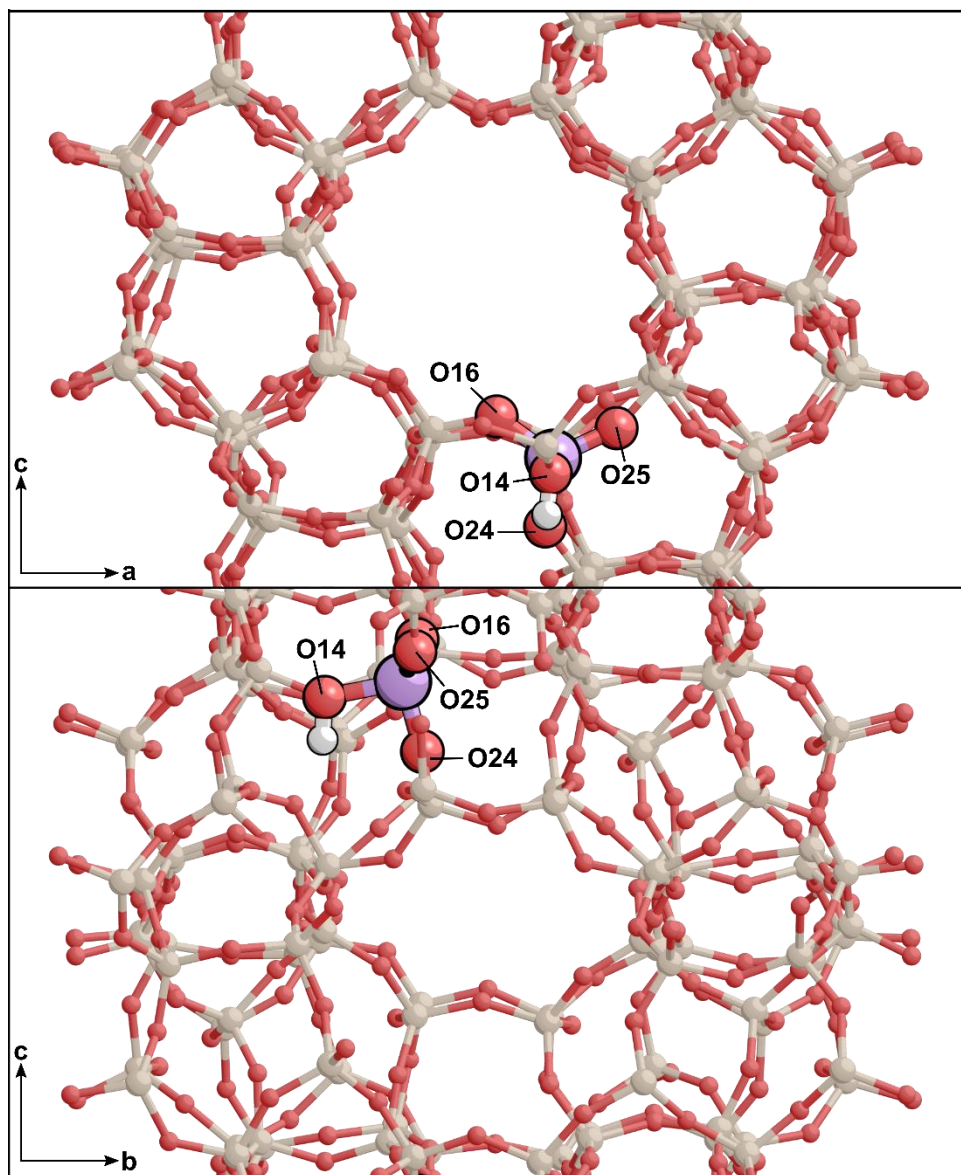
**Figure S5.** Different orientations of the benzene ring and surface methylation transition state during surface methylation near benzene. Bond distances between Al–O---CH<sub>3</sub> and CH<sub>3</sub>---OCH<sub>3</sub>H are shown in Angstroms. Views are shown down the straight (top) and sinusoidal (bottom) channels. Relative electronic energy values (kJ mol<sup>-1</sup>) are reported relative to the most stable structure.



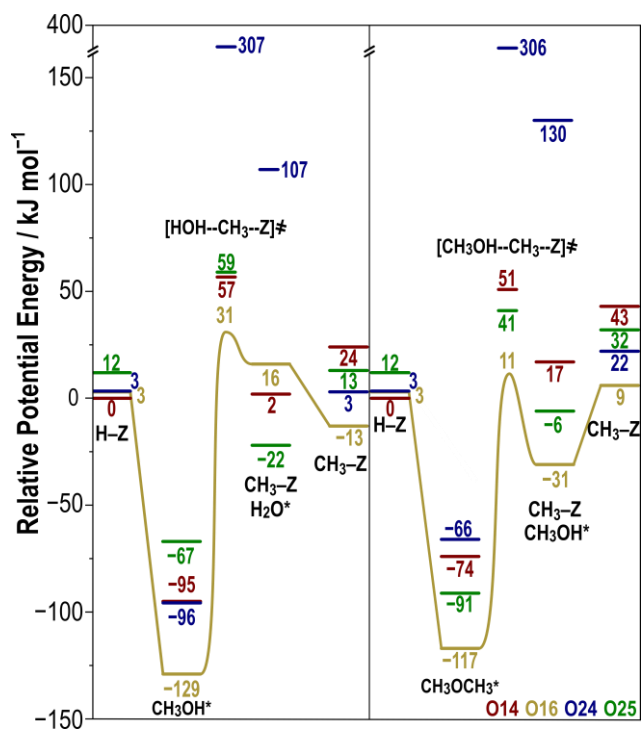
**Figure S6.** Energy (orange) and free energy (blue) of all optimized benzene re-orientations. Energies are relative to the state with the lowest free energy.



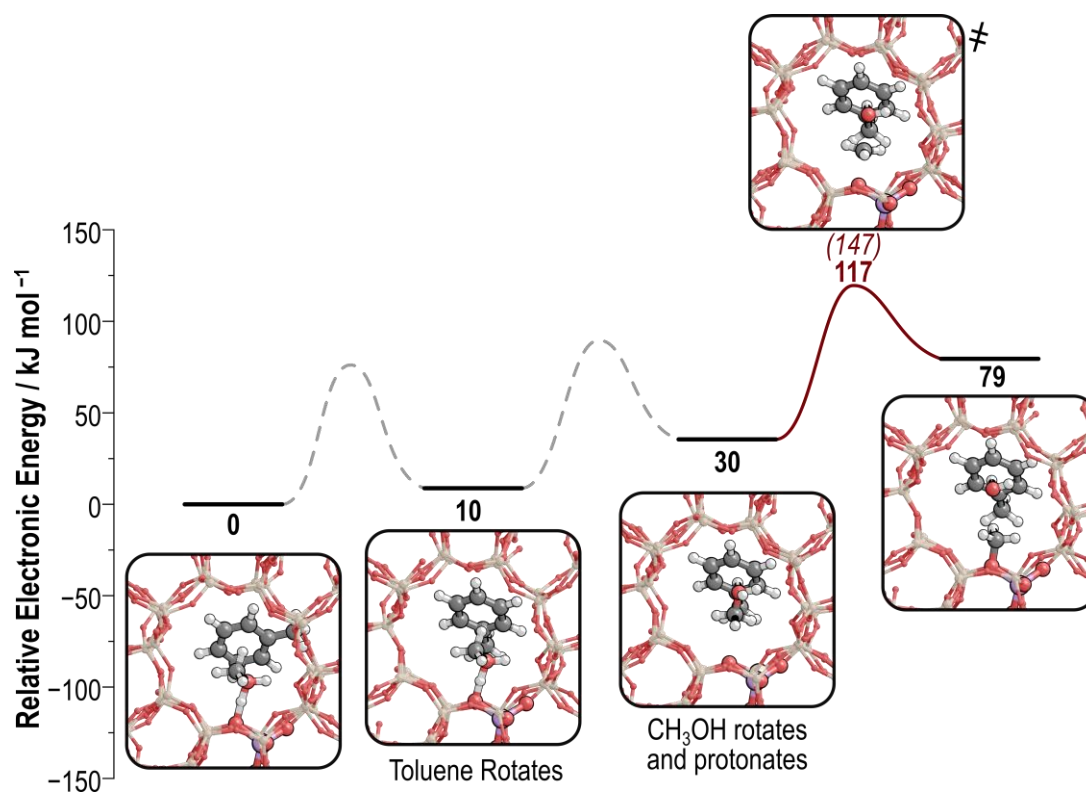
**Figure S7.** Energy (orange) and free energy (gray) of all optimized surface methylation near 1,2,4-trimethylbenzene transition states relative to the state with the lowest free energy.



**Figure S8.** The location of each O-site at the T11 site in MFI along the straight (top) and sinusoidal (bottom) pores.

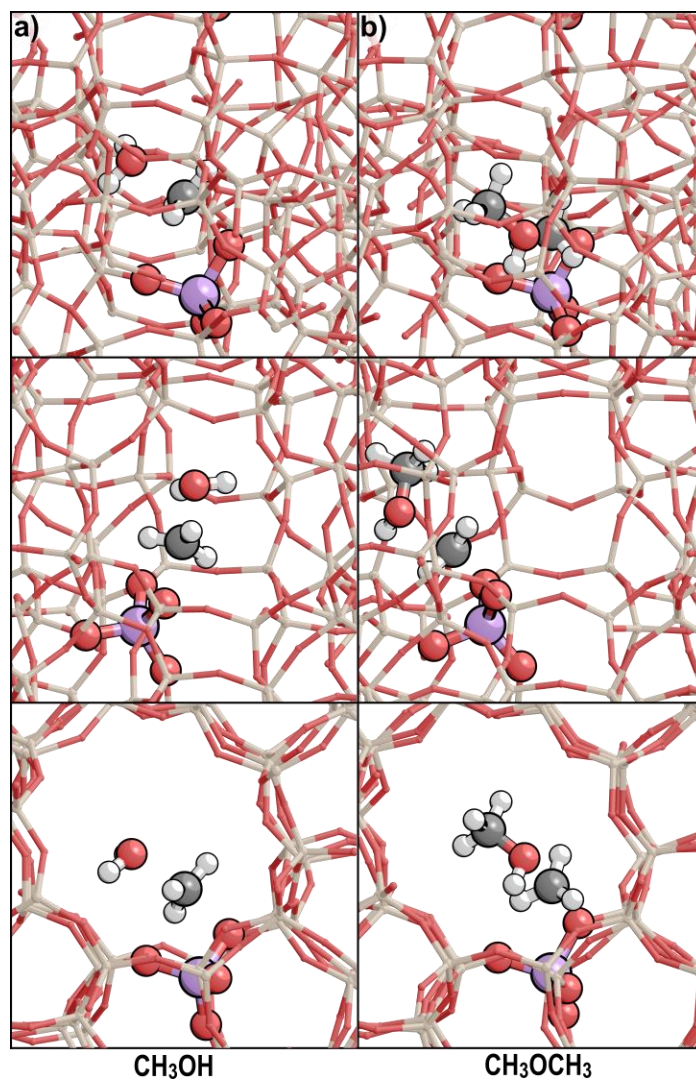


**Figure S9.** Reaction coordinate diagram of initial surface methylation energies (pre-reorientation) at O14 (red), O16 (yellow), O24 (blue), and O25 (green) with CH<sub>3</sub>OH (left) and CH<sub>3</sub>OCH<sub>3</sub> (right). The most favorable pathway determined by the lowest energy transition state occurs at O16 and is traced with lines. Potential energy values (kJ mol<sup>-1</sup>) are relative to a proton on O14. Initial trends show energies increase as O16 < O14 < O25 < O24 with CH<sub>3</sub>OH and O16 < O25 < O14 < O24 with CH<sub>3</sub>OCH<sub>3</sub>.

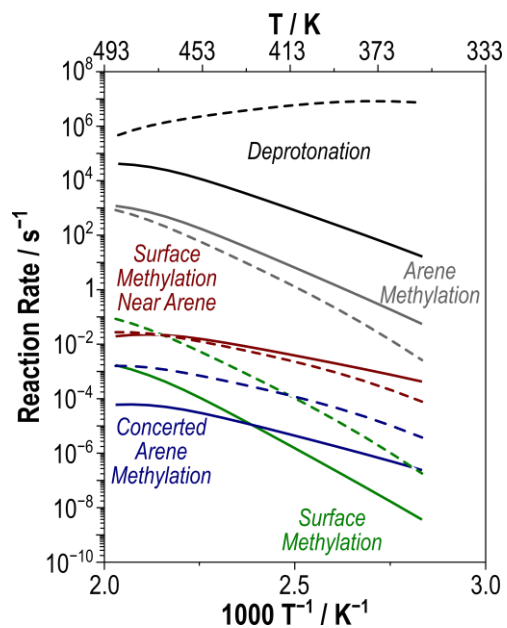


**Figure S10.** Electronic energies of toluene reorientation from the most stable reactant state to the orientation of the transition state. Reorientation barriers are estimated to be significantly less than the intrinsic barrier of surface methylation ( $147 \text{ kJ mol}^{-1}$ ), suggesting that they are kinetically irrelevant.



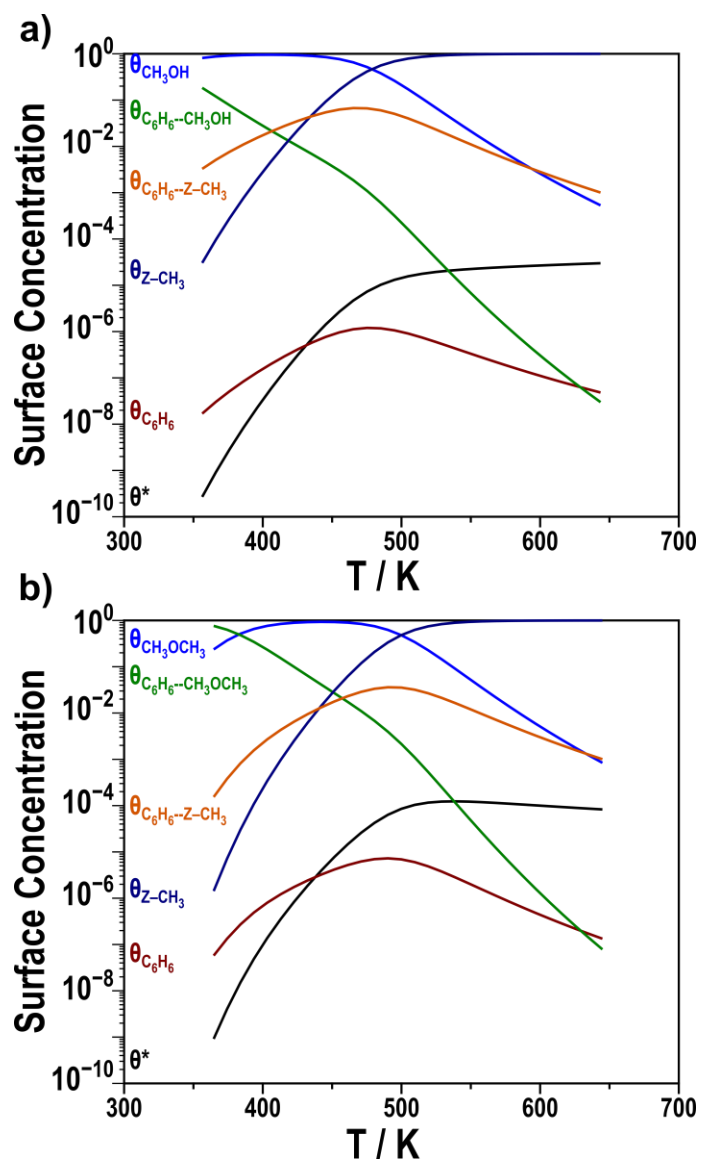


**Figure S11.** Extra views of surface methylation transition states without a spectating arene at O24 using **a)**  $\text{CH}_3\text{OH}$  and **b)**  $\text{CH}_3\text{OCH}_3$ .

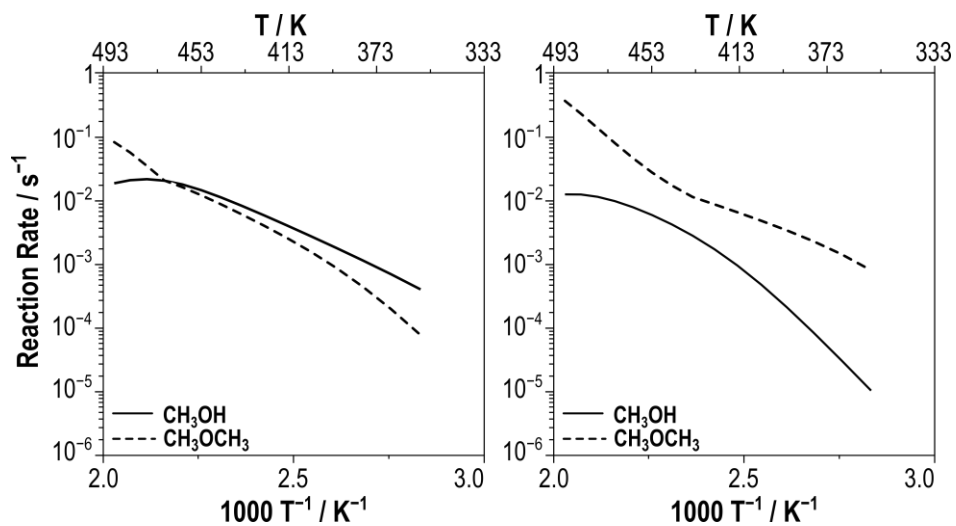


**Figure S12.** Rates of surface methylation (green), concerted methylation (blue), surface methylation near benzene (red), arene methylation (gray), and deprotonation of  $\text{C}_7\text{H}_9^+$  to toluene with  $\text{CH}_3\text{OH}$  (solid) and  $\text{CH}_3\text{OCH}_3$  (dashed). Rates are reported at 0.68 bar  $\text{CH}_3\text{OR}$ , 0.02 bar  $\text{C}_6\text{H}_6$ , 0.1%  $\text{C}_6\text{H}_6$  conversion, from 353–493 K.

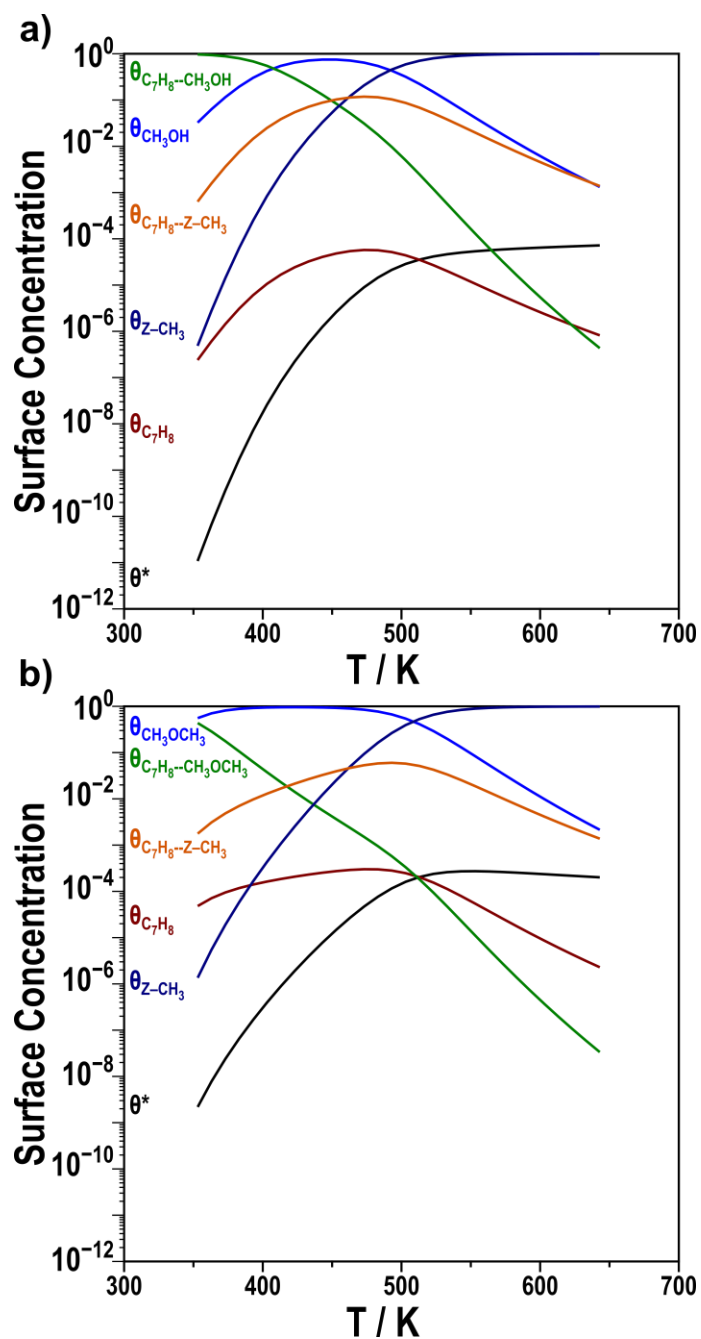




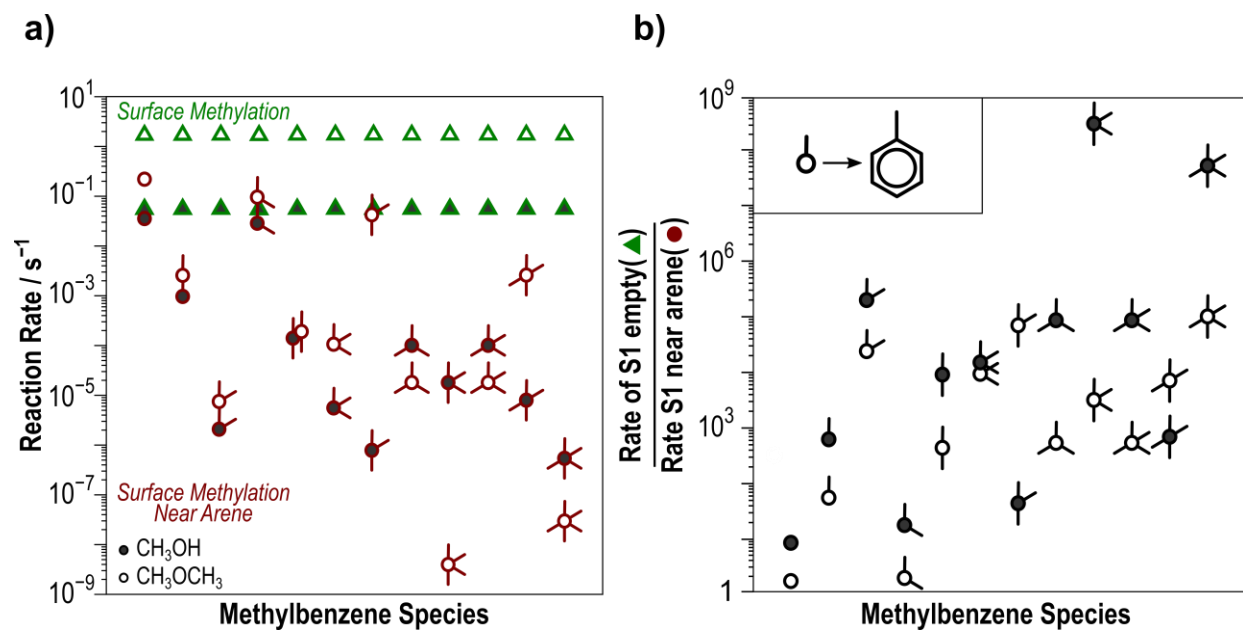
**Figure S13.** Evolution of surface species during benzene methylation with a)  $\text{CH}_3\text{OH}$  and b)  $\text{CH}_3\text{OCH}_3$  from 353–653 K, 0.68 bar  $\text{CH}_3\text{OH}$ , 0.02 bar  $\text{C}_6\text{H}_6$ , 0.1%  $\text{C}_6\text{H}_6$  conversion.



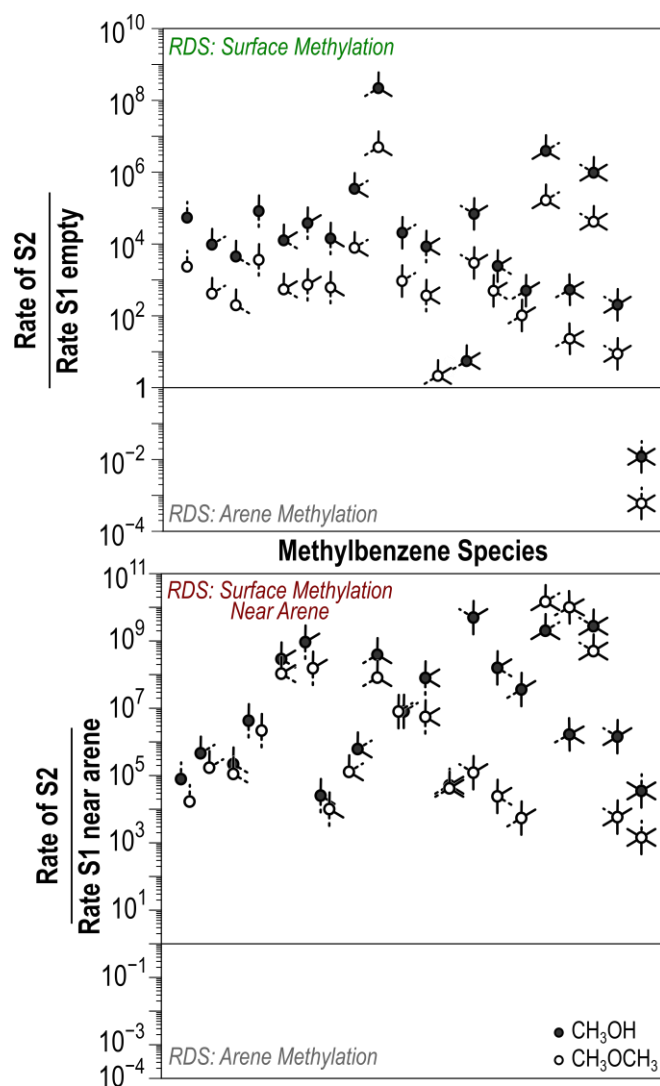
**Figure S14.** Overall rates of **a)**  $\text{C}_6\text{H}_6$  and **b)**  $\text{C}_7\text{H}_8$  methylation with  $\text{CH}_3\text{OH}$  (solid) and  $\text{CH}_3\text{OCH}_3$  (dashed) between 353 K and 493 K, 0.68 bar  $\text{CH}_3\text{OR}$ , 0.02  $\text{C}_6\text{H}_6$  and 0.03 bar  $\text{C}_7\text{H}_8$  0.1% conversion.



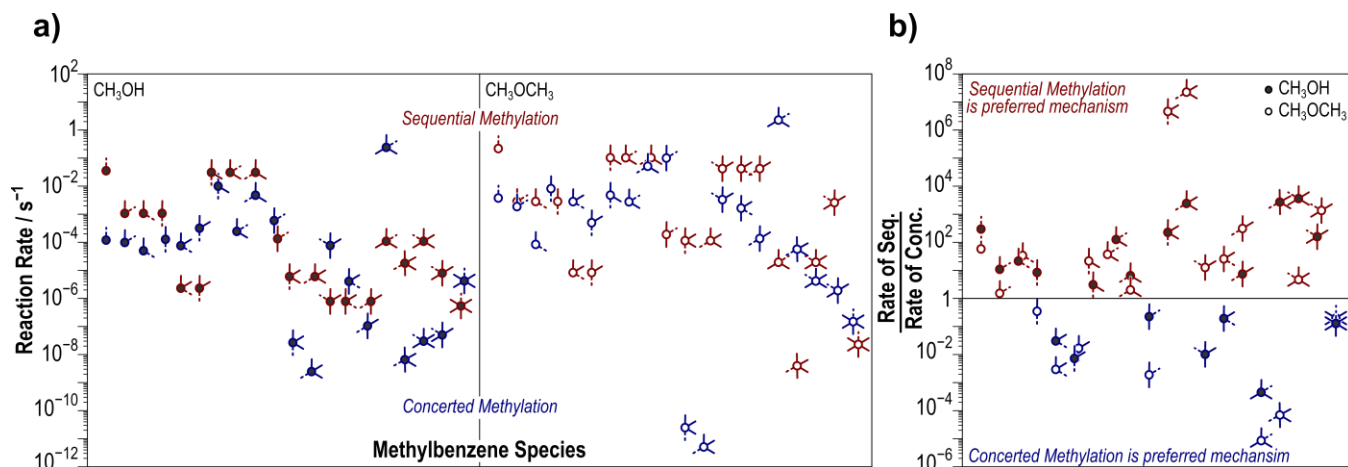
**Figure S15.** Evolution of surface species with a) CH<sub>3</sub>OH and b) CH<sub>3</sub>OCH<sub>3</sub> from 353–653 K, 0.68 bar CH<sub>3</sub>OH, 0.03 bar C<sub>7</sub>H<sub>8</sub>, 0.1% C<sub>7</sub>H<sub>8</sub> conversion.



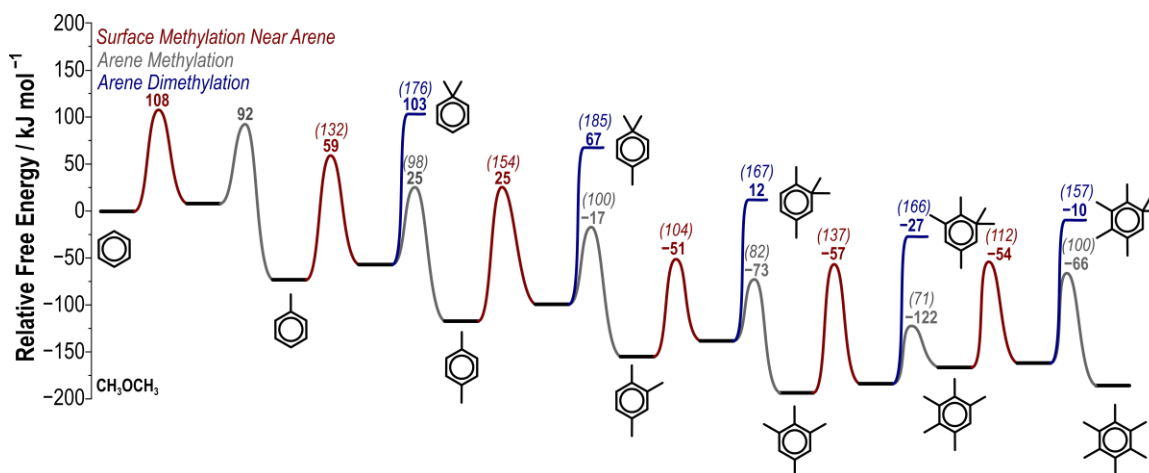
**Figure S16.** **a)** Maximum rate of surface methylation in an empty pore (green, triangles) and surface methylation with a spectating arene (red, circle) with CH<sub>3</sub>OH (filled) and CH<sub>3</sub>OCH<sub>3</sub> (empty), and **b)** ratio of the rate of surface methylation in an empty pore to the rate of surface methylation near arene with CH<sub>3</sub>OH (filled) and CH<sub>3</sub>OCH<sub>3</sub> (empty). Rates are reported at 0.04 bar C<sub>x</sub>H<sub>y</sub>, 0.08 bar CH<sub>3</sub>OR, 10% aromatic conversion, and 623 K.



**Figure S17.** Ratio of ring methylation (second step of the sequential mechanism) maximum rate to rate of surface methylation (first step of the sequential mechanism) in an empty pore (top) and near a spectating arene (bottom) with  $\text{CH}_3\text{OH}$  (filled) and  $\text{CH}_3\text{OCH}_3$  (empty). Values above 1 (horizontal gray line) signify that the surface methylation step is rate-determining while values below 1 signify arene methylation is rate-determining. Dashed lines represent the location of methyl-addition on the arene. Rates are reported at 0.04 bar  $\text{C}_x\text{H}_y$ , 0.08 bar  $\text{CH}_3\text{OR}$ , 10% aromatic conversion, and 623 K.



**Figure S18.** a) Rates of sequential (red) and concerted (blue) methylation with  $\text{CH}_3\text{OH}$  (filled) and  $\text{CH}_3\text{OCH}_3$  (empty), and b) a ratio of concerted and sequential methylation rates. Rates are reported at 0.04 bar  $\text{C}_x\text{H}_y$ , 0.08 bar  $\text{CH}_3\text{OR}$ , 10% aromatic conversion, and 623 K.



**Figure S19.** Reaction coordinate diagram showing sequential methylation barriers compared to geminal methylation barriers via methylation by  $\text{CH}_3\text{-Z}$  at 623K.

## S2. Maximum Rate analysis of Arene Methylation Rates

Maximum rate analyses assert, one at a time, that a step is rate-determining and that all preceding steps are quasi-equilibrated. Maximum rate analysis permits identification of the rate-determining step (that with the lowest maximum rate in a pathway) and allows for direct comparison of experimentally obtained rates to those obtained from DFT. All rates are determined from transition state theory with activation entropies contributing to pre-exponential factors. Rate equations are derived based on the assumption of a single adsorption site that may contain isolated species (such as  $\text{CH}_3\text{OR}^*$  or  $\text{C}_x\text{H}_y^*$ ) or complexes in which two species are adsorbed concurrently (such as  $\text{C}_x\text{H}_y\text{-CH}_3\text{OR}^*$ , which represents  $\text{CH}_3\text{OH}$  or  $\text{CH}_3\text{OCH}_3$  and an arene present in the pore). All adsorption steps are assumed to be quasi-equilibrated and are represented by equilibrium constants as defined in Fig. 6.

Several potential site-occupying intermediates are considered in this analysis:  $\text{CH}_3\text{OR}^*$ ,  $\text{C}_x\text{H}_y^*$ ,  $\text{CH}_3\text{-Z}$ ,  $\text{C}_x\text{H}_y\text{-CH}_3\text{OR}^*$ , and  $\text{C}_x\text{H}_y\text{-CH}_3\text{-Z}$  where the final two intermediates represent arenes co-adsorbed with  $\text{CH}_3\text{OR}^*$  or  $\text{CH}_3\text{-Z}$  (Fig. 6). A site-balance can then be described as:

$$\frac{[*]}{[L]} = \left( 1 + K_{\text{CH}_3\text{OR}}(\text{CH}_3\text{OR}) + K_{\text{C}_x\text{H}_y}(\text{C}_x\text{H}_y) + K'_{\text{S1}}K'_{\text{C}_x\text{H}_y}(\text{CH}_3\text{OR})(\text{C}_x\text{H}_y) + K_{\text{S1}}K_{\text{CH}_3\text{OR}}(K_{\text{ROH}})^{-1} \frac{(\text{CH}_3\text{OR})}{(\text{ROH})} + K'_{\text{S1}}K_{\text{CH}_3\text{OR}}K'_{\text{C}_x\text{H}_y}(K_{\text{ROH}})^{-1} \frac{(\text{CH}_3\text{OR})(\text{C}_x\text{H}_y)}{(\text{ROH})} \right)^{-1} \quad (\text{S1})$$

where species in parentheses indicate partial pressures and equilibrium constants are defined in Fig. 6 in the main text. The  $[*]$  term represents the concentration of unoccupied sites in the zeolite, and  $[L]$  represents all possible sites, regardless of their state (bare or occupied by guest species).

For the concerted methylation mechanism, there are three reaction steps: the adsorption of the methylating agent,  $\text{CH}_3\text{OR}$ , ( $K_{\text{CH}_3\text{OR}}$ , Eq. S2), the co-adsorption of the arene species to form a coordinated complex between the arene and methylating agent,  $\text{CH}_3\text{OR} - \text{C}_x\text{H}_y^*$ , ( $K'_{\text{C}_x\text{H}_y}$ , Eq. S3), and the methylation of the arene species ( $k$ , Eq. S4)



The product formation rate is simply the rate of depletion of the arene-methylating agent complex:

$$r = k_c [\text{CH}_3\text{OR} - \text{C}_x\text{H}_y^*] \quad (\text{S5})$$

The rate can be described in terms of partial pressures of each reactant species by combining with Eq. S2–S3 with Eq. S5:

$$r = K_{\text{CH}_3\text{OR}}K'_{\text{C}_x\text{H}_y}k_c(\text{C}_x\text{H}_y)(\text{CH}_3\text{OR})[*] \quad (\text{S6})$$

Normalizing by the number of sites  $[L]$  yields a turnover rate for concerted methylation, yielding a general form of the rate equation for concerted arene methylation:

$$\frac{r}{L} = k_c K'_{\text{C}_x\text{H}_y} K_{\text{CH}_3\text{OR}} (\text{CH}_3\text{OR})(\text{C}_x\text{H}_y) \left( \frac{[*]}{[L]} \right) \quad (\text{S7})$$

This form of the equation assumes no prior methylation to form the arene occurs and that the arene simply adsorbs prior to reaction.

In the sequential mechanism, there are four reaction steps: adsorption of the methylating agent (Eq. S8), methylation of the acid site (Eq. S9), adsorption of the arene species (Eq. S10), and methylation of the arene (Eq. S11). Several rate equations can be derived depending on which reaction step is rate determining. If surface methylation is rate determining, i.e.:



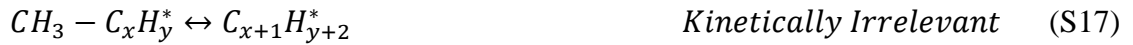
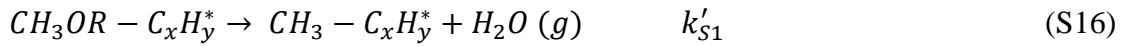
where steps labeled “kinetically irrelevant” need not be considered in kinetic analysis as they occur after the rate-determining step. In this case, the arene methylation rate is simply dependent on the concentration of adsorbed  $\text{CH}_3\text{OH}$  or  $\text{CH}_3\text{OCH}_3$ :

$$r = k_{S1}[\text{CH}_3\text{OR}^*] \quad (\text{S12})$$

When expressed in terms of reactant pressures and normalized by the number of sites, the turnover rate becomes:

$$\frac{r}{L} = k_{S1}K_{\text{CH}_3\text{OR}}(\text{CH}_3\text{OR})\left(\frac{[*]}{[L]}\right) \quad (\text{S13})$$

Surface methylation in the sequential pathway can also occur in the presence of a co-adsorbed arene species. Arene adsorption in this pathway occurs after the methylating agent adsorbs but before the surface methoxy group is formed. If surface methylation in the presence of an arene species is the rate determining step (RDS), the mechanism becomes:



Then the rate becomes dependent on the concentration of the complex formed by co-adsorbed arene and  $\text{CH}_3\text{OR}$ :

$$r = k'_{S1}[\text{CH}_3\text{OR} - \text{C}_x\text{H}_y^*] \quad (\text{S18})$$

And in terms of reactant pressures the turnover rate is:

$$\frac{r}{L} = k'_{S1}K'_{\text{C}_x\text{H}_y}K_{\text{CH}_3\text{OR}}(\text{CH}_3\text{OR})(\text{C}_x\text{H}_y)\left(\frac{[*]}{[L]}\right) \quad (\text{S19})$$

Finally, if arene methylation is the rate determining step in the sequential mechanism, then the coefficients for the mechanism become



The rate, therefore, becomes dependent on the coverage of adsorbed arene near surface methoxy species.

$$r = k_{S2}[\text{CH}_3 - \text{C}_x\text{H}_y^*] \quad (\text{S24})$$

$$r = k_{S2}K_{\text{CH}_3\text{OR}}(K_{\text{ROH}})^{-1}K'_{\text{C}_x\text{H}_y}K_1'(\text{C}_x\text{H}_y)(\text{CH}_3\text{OR})(\text{HOR})^{-1}[*] \quad (\text{S25})$$



Where  $K_{ROH}$  represents the desorption of water when  $CH_3-C_xH_y$  is present in the pore. When the rate is normalized per site, the turnover rate becomes:

$$\frac{r}{L} = k_{S2} K_{CH_3OR} (K_{ROH})^{-1} K''_{C_xH_y} K_1 (C_xH_y) (CH_3OR) (ROH)^{-1} \left( \frac{[*]}{[L]} \right) \quad (S26)$$

The concentration of each species can be expressed in terms of conversion, as shown in Table S1.

**Table S1.** Mole balance expressions for each species expressed in terms of pressure and conversion.

Species	Initial	Change	Remaining
$C_xH_y$	$P_{C_xH_y,0}$	$-P_{C_xH_y,0}X$	$P_{C_xH_y,0}(1-X)$
$CH_3OR$	$\frac{P_{CH_3OR,0}}{P_{C_xH_y,0}} P_{C_xH_y,0}$	$-P_{C_xH_y,0}X$	$P_{C_xH_y,0} \left( \frac{P_{CH_3OR}}{P_{C_xH_y}} - X \right)$
$ROH$	0	$-P_{C_xH_y,0}X$	$-P_{C_xH_y,0}X$

Substituting into the expressions for methylation rate for each mechanism and RDS:

$$\frac{[*]}{[L]} = \left( 1 + K_{CH_3OR} P_{C_xH_y} \left( \frac{P_{CH_3OR}}{P_{C_xH_y}} - X \right) + K_{C_xH_y} P_{C_xH_y} (1-X) + K_{CH_3OR} K'_{C_6H_6} P_{C_xH_y,0}^2 (1-X) \left( \frac{P_{CH_3OR}}{P_{C_xH_y}} - X \right) + K_{CH_3OR} K_1 (K_{ROH})^{-1} P_{C_xH_y,0} \frac{(1-X)}{X} + K_{CH_3OR} K'_{C_6H_6} K_1 (K_{ROH})^{-1} P_{C_xH_y,0} \frac{(1-X) \left( \frac{P_{CH_3OR}}{P_{C_xH_y}} - X \right)}{X} \right)^{-1} \quad (S27)$$

The rate equations for each possible RDS can also be expressed in terms of conversion. The rate equations when surface methylation in the absence of co-adsorbed arene is the RDS becomes

$$r = k_{S1} K_{CH_3OR} P_{C_xH_y,0} (1-X) \quad (S28)$$

When arene adsorption occurs before surface methylation, but surface methylation is still the RDS, the rate equations becomes:

$$r = k'_{S1} K_{CH_3OR} K'_{C_6H_6} P_{C_xH_y,0} \left( \frac{P_{C_xH_y,0}}{P_{CH_3OR,0}} - X \right) \quad (S29)$$

However, if arene methylation is the RDS, then the rate equation based on conversion becomes:

$$r = k_{S2} K_{CH_3OR} K'_{S1} K'_{C_6H_6} (K'_{ROH})^{-1} P_{C_xH_y,0} \frac{(1-X) \left( \frac{P_{CH_3OR,0}}{P_{C_xH_y,0}} - X \right)}{X} \quad (S30)$$

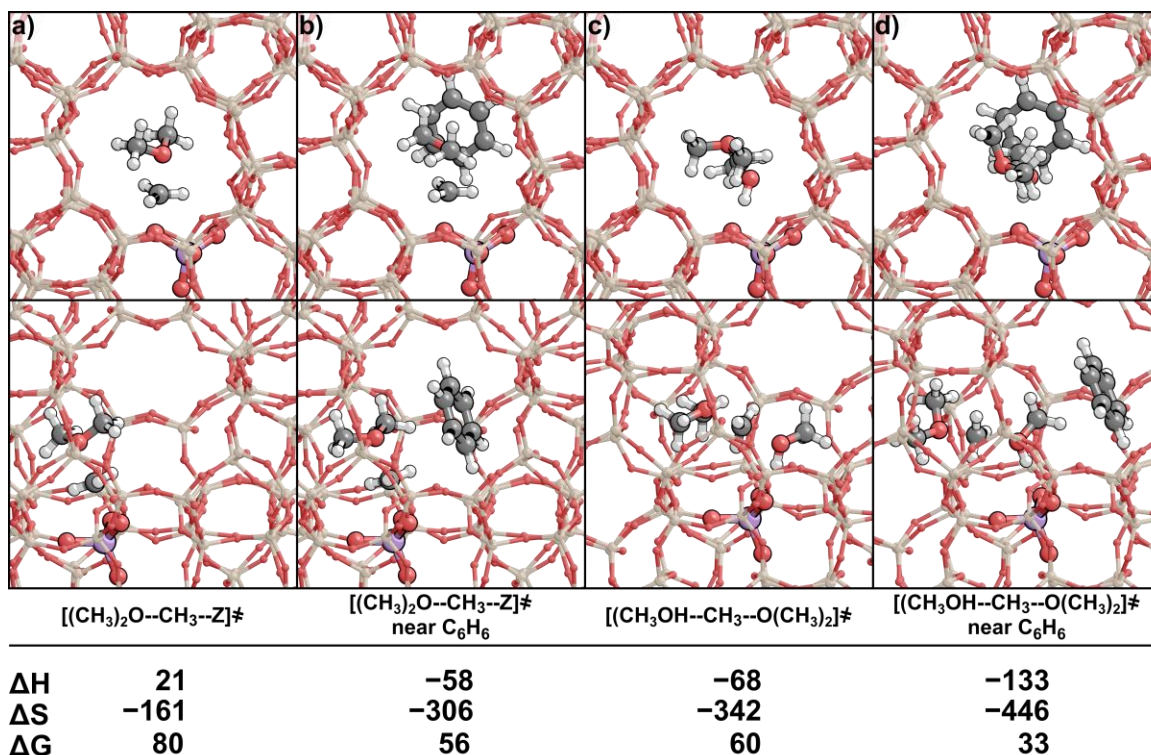
Finally, if the concerted pathway prevails, then the rate equation follows as:

$$r = k_C K_{CH_3OR} K'_{C_6H_6} P_{C_xH_y,0} (1-X) \left( \frac{P_{CH_3OR,0}}{P_{C_xH_y,0}} - X \right) \quad (S31)$$

### S3. Trimethyloxonium Formation

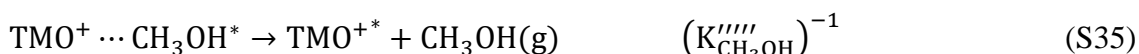
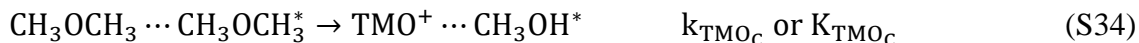
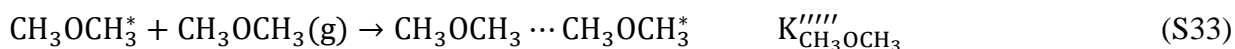
There are two mechanisms through which trimethyloxonium (TMO) species can form: a two-step mechanism in which the surface is first methylated by  $CH_3OCH_3$  and a second  $CH_3OCH_3$  is subsequently methylated by  $CH_3-Z$  (Figure S15a–b). Or a one-step mechanism in which two  $CH_3OCH_3$  directly react to form TMO (Figure S15c–d). Once TMO species are formed, it is

possible that they will contribute to methylation of the zeolite surface or the arene. We have employed maximum rate analyses to compare the rates of these TMO formation mechanisms and evaluate their contributions to benzene methylation.



**Figure S20.** The transition state structure of trimethyloxonium formation from methylation by  $\text{CH}_3\text{-Z}$  in a) in an empty pore and b) with a spectating benzene and via reaction of two  $\text{CH}_3\text{OCH}_3$  in a) an empty pore and b) with spectating benzene. Views are presented down the straight (top) and sinusoidal (bottom) channels. Enthalpy ( $\text{kJ mol}^{-1}$ ), entropy ( $\text{J mol}^{-1} \text{K}^{-1}$ ), and free energy ( $\text{kJ mol}^{-1}$ ) are reported at 373 K and 1 bar.

There are 3 possible rate-determining steps in the one-step TMO formation mechanism that we will analyze with maximum rate analysis. The first is formation of TMO from the reaction of two  $\text{CH}_3\text{OCH}_3$  molecules



The rate of this reaction can be expressed by

$$r = K_{\text{CH}_3\text{OCH}_3} K_{\text{CH}_3\text{OCH}_3}''' k_{\text{TMOc}} (\text{CH}_3\text{OCH}_3)^2 \frac{[*]}{\text{L}} \quad (\text{S36})$$

After the formation of TMO, it can either methylate the zeolite surface



Which has rate

$$r = K_{\text{CH}_3\text{OCH}_3} K_{\text{CH}_3\text{OCH}_3}^{\prime\prime\prime\prime} K_{\text{TMO}_c} (K_{\text{CH}_3\text{OH}}^{\prime\prime\prime\prime})^{-1} k_{\text{TMO}_{\text{SM}}} \frac{(\text{CH}_3\text{OCH}_3)^2}{(\text{CH}_3\text{OH})} \frac{[*]}{L} \quad (\text{S38})$$

Or it can methylate a benzene ring



Leading to a rate of

$$r = K_{\text{CH}_3\text{OCH}_3} K_{\text{CH}_3\text{OCH}_3}^{\prime\prime\prime\prime} K_{\text{TMO}_c} (K_{\text{CH}_3\text{OH}}^{\prime\prime\prime\prime})^{-1} K_{\text{C}_6\text{H}_6}^{\prime\prime\prime} k_{\text{TMO}_m} \frac{(\text{CH}_3\text{OCH}_3)^2 (\text{C}_6\text{H}_6)}{(\text{CH}_3\text{OH})} \frac{[*]}{L} \quad (\text{S41})$$

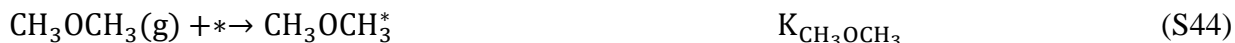
Alternatively, the elementary steps S32–S37 can occur with spectating benzene changing equation S36 to

$$r = K_{\text{CH}_3\text{OCH}_3} K_{\text{CH}_3\text{OCH}_3}^{\prime\prime\prime\prime} K_{\text{C}_6\text{H}_6}^{\prime\prime\prime} k_{\text{TMO}_c}' (\text{CH}_3\text{OCH}_3)^2 (\text{C}_6\text{H}_6) \frac{[*]}{L} \quad (\text{S42})$$

And equation S38 becomes

$$r = K_{\text{CH}_3\text{OCH}_3} K_{\text{CH}_3\text{OCH}_3}^{\prime\prime\prime\prime} K_{\text{C}_6\text{H}_6}^{\prime\prime\prime} K_{\text{TMO}_c} (K_{\text{CH}_3\text{OH}}^{\prime\prime\prime\prime})^{-1} k_{\text{TMO}_{\text{SM}}} \frac{(\text{CH}_3\text{OCH}_3)^2 (\text{C}_6\text{H}_6)}{(\text{CH}_3\text{OH})} \frac{[*]}{L} \quad (\text{S43})$$

The two-step TMO formation mechanism also has three possible rate-determining steps. The first is formation of  $\text{CH}_3\text{-Z}$  species, similar the previously describe sequential arene methylation mechanism



This reaction occurs with a rate of

$$r = K_{\text{CH}_3\text{OCH}_3} k (\text{CH}_3\text{OCH}_3) \frac{[*]}{L} \quad (\text{S47})$$

Once the  $\text{CH}_3\text{-Z}$  species is formed, it can react with a second  $\text{CH}_3\text{OCH}_3$  molecule to form TMO



$$r = K_{\text{CH}_3\text{OCH}_3} K_{\text{S1}} (K_{\text{CH}_3\text{OH}}^{\prime\prime})^{-1} K_{\text{CH}_3\text{OCH}_3}^{\prime\prime\prime\prime} k_{\text{TMO}_s} \frac{(\text{CH}_3\text{OCH}_3)^2}{(\text{CH}_3\text{OH})} \frac{[*]}{L} \quad (\text{S50})$$

Finally, the TMO can methylate benzene to form toluene





$$r = K_{\text{CH}_3\text{OCH}_3} K_{\text{S1}} (K''_{\text{CH}_3\text{OH}})^{-1} K''''_{\text{CH}_3\text{OCH}_3} K_{\text{TMO}_s} K'''_{\text{C}_6\text{H}_6} k_{\text{TMO}_m} \frac{(\text{CH}_3\text{OCH}_3)^2 (\text{C}_6\text{H}_6) \frac{[*]}{\text{L}}}{(\text{CH}_3\text{OH})} \quad (\text{S53})$$

Similar to the one-step mechanism, the first two rate-determining steps can also occur with spectating benzene changing the rate equation of Eq. S47 to

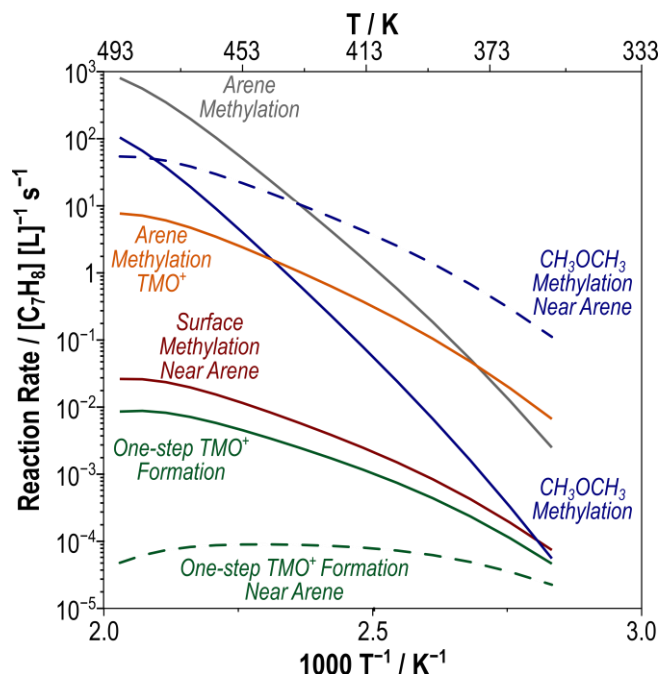
$$r = K_{\text{CH}_3\text{OCH}_3} K''_{\text{C}_6\text{H}_6} k'_{\text{S1}} (\text{CH}_3\text{OCH}_3) (\text{C}_6\text{H}_6) \frac{[*]}{\text{L}} \quad (\text{S54})$$

And Eq. S50 becomes

$$r = K_{\text{CH}_3\text{OCH}_3} K''_{\text{C}_6\text{H}_6} K'_{\text{S1}} (K'''_{\text{CH}_3\text{OH}})^{-1} K''''_{\text{CH}_3\text{OCH}_3} k'_{\text{TMO}_s} \frac{(\text{CH}_3\text{OCH}_3)^2 (\text{C}_6\text{H}_6) \frac{[*]}{\text{L}}}{(\text{CH}_3\text{OH})} \quad (\text{S55})$$

Using these rate equations, we can evaluate the rates of these reaction pathways and compare them to the arene methylation pathways discussed in Section S2.

Section 3 of the manuscript demonstrated that surface methylation with spectating benzene occurs with higher rates than surface methylation in an empty pore; therefore, only surface methylation with spectating benzene is considered in this discussion. Rates of the one-step mechanism are lower than surface methylation with spectating benzene, suggesting that this one-step TMO formation mechanism is not kinetically relevant. Similar to surface methylation, the intrinsic barrier of TMO formation via methylation of  $\text{CH}_3\text{OCH}_3$  by  $\text{CH}_3\text{-Z}$  is lowered by  $10 \text{ kJ mol}^{-1}$  (from  $82 \text{ kJ mol}^{-1}$  to  $72 \text{ kJ mol}^{-1}$ ) and thus TMO formation via the sequential mechanism occurs with higher rates when benzene is present (Figure S16). At temperatures below 423 K, the reaction of  $\text{CH}_3\text{-Z}$  species with  $\text{CH}_3\text{OCH}_3$  occurs at a higher rate than reaction of  $\text{CH}_3\text{-Z}$  with  $\text{C}_6\text{H}_6$  to form toluene; therefore, at low temperatures we predict methylation by TMO is contributing to the formation of  $\text{C}_7\text{H}_8$  species. However, the rate of  $\text{C}_6\text{H}_6$  methylation by  $\text{CH}_3\text{-Z}$ , the formation of TMO by  $\text{CH}_3\text{OCH}_3$  reaction with  $\text{CH}_3\text{-Z}$ , and  $\text{C}_6\text{H}_6$  methylation by TMO are all facile compared to the formation of  $\text{CH}_3\text{-Z}$  species indicating that the overall rate of sequential methylation is not significantly impacted when considering this additional sequential TMO route.



**Figure S21.** Rates of surface methylation ( $\text{CH}_3\text{-Z}$  formation) with  $\text{CH}_3\text{OCH}_3$  and spectating benzene (red), reaction of two  $\text{CH}_3\text{OCH}_3$  to form TMO in an empty pore (green, solid) and with spectating benzene (green, dashed), methylation of  $\text{CH}_3\text{OCH}_3$  with  $\text{Z-CH}_3$  in an empty pore (blue, solid) and with spectating benzene (blue, dashed), arene methylation with  $\text{CH}_3\text{-Z}$  (gray), and arene methylation with TMO (orange). Rates are shown at 373 K, 0.02 bar  $\text{C}_6\text{H}_6$ , 0.68 bar  $\text{CH}_3\text{OCH}_3$ , and 0.1% aromatic conversion.

#### S4. Reaction and Transition State Energies

**Table S2.** Adsorption enthalpy and entropy of methylbenzene species

Species	$\Delta H_{\text{ads}}^a$ $\text{kJ mol}^{-1}$	$\Delta S_{\text{ads}}$ $\text{J mol}^{-1} \text{K}^{-1}$
Benzene	-66.8	-123.2
Toluene	-92.9	-155.8
<i>ortho</i> -xylene	-90.7	-166.7
<i>meta</i> -xylene	-94.6	-183.9
<i>para</i> -xylene	-86.8	-161.6
1,2,3-trimethylbenzene	-87.2	-183.7
1,2,4-trimethylbenzene	-96.8	-204.1
1,3,5-trimethylbenzene	-97.4	-157.5
1,2,3,4-tetramethylbenzene	-101.2	-195.2
1,2,3,5-tetramethylbenzene	-80.8	-185.6
1,2,4,5-tetramethylbenzene	-71.8	-208.6
Pentamethylbenzene	-44.5	-225.3
Hexamethylbenzene	-43.5	-236.1

<sup>a</sup> $\Delta H_{\text{ads}}$  values are reported at 473 K

**Table S3.** Reaction and activation barriers of surface methylation.

Spectating Species	Methylation Agent							
	CH <sub>3</sub> OH				CH <sub>3</sub> OCH <sub>3</sub>			
	$\Delta H_{act}^a$ kJ mol <sup>-1</sup>	$\Delta S_{act}$ J mol <sup>-1</sup> K <sup>-1</sup>	$\Delta H_{rxn}^a$ kJ mol <sup>-1</sup>	$\Delta S_{rxn}$ J mol <sup>-1</sup> K <sup>-1</sup>	$\Delta H_{act}^a$ kJ mol <sup>-1</sup>	$\Delta S_{act}$ J mol <sup>-1</sup> K <sup>-1</sup>	$\Delta H_{rxn}^a$ kJ mol <sup>-1</sup>	$\Delta S_{rxn}$ J mol <sup>-1</sup> K <sup>-1</sup>
Empty	144.1	1.1	88.9	47.8	124.7	-10.8	82.4	23.0
Benzene	102.3	-7.6	68.8	21.8	118.2	11.6	83.3	37.8
Toluene	117.5	-18.0	85.4	18.6	112.2	-5.3	98.9	13.0
<i>ortho</i> -xylene	130.7	-32.5	103.3	10.6	134.1	-16.0	123.9	-1.1
<i>meta</i> -xylene	114.8	-11.5	82.5	30.4	129.4	18.1	107.1	35.7
<i>para</i> -xylene	135.7	-1.3	105.1	27.4	148.1	8.3	148.7	15.2
1,2,3-tri	114.9	-5.4	86.1	32.9	124.4	11.9	108.5	21.3
1,2,4-tri	126.6	-14.9	96.4	24.1	124.8	4.0	95.2	34.0
1,3,5-tri	110.1	-22.4	82.4	22.4	135.0	3.9	106.4	29.2
1,2,3,4-tetra	104.9	-22.8	111.7	21.1	140.2	-17.8	78.8	38.6
1,2,3,5-tetra	105.3	1.1	79.2	28.9	120.0	-13.4	88.7	5.9
1,2,4,5-tetra	105.1	-3.6	87.1	39.8	129.6	31.5	122.9	20.4
Penta	93.5	-10.3	66.8	21.6	109.8	-27.3	55.1	13.5

<sup>a</sup> $\Delta H_{act}$  and  $\Delta H_{rxn}$  are reported at 473 K**Table S4.** Activation Energy of surface methylation transition states.

Reactants	Products	$\Delta H_{act}^a$ kJ mol <sup>-1</sup>	$\Delta S_{act}^a$ J mol <sup>-1</sup> K <sup>-1</sup>
Benzene	Toluene	71.4	-20.8
Toluene	<i>Ortho</i>	75.0	-25.1
Toluene	<i>Meta</i>	83.3	-20.5
Toluene	<i>Para</i>	71.0	-17.3
<i>Ortho</i>	1,2,3-tri	70.5	-18.9
<i>Ortho</i>	1,2,4-tri	66.3	-21.4
<i>Meta</i>	1,3,5-tri	64.4	-38.7
<i>Meta</i>	1,2,3-tri	62.2	-27.3
<i>Meta</i>	1,2,4-tri	33.3	-22.3
<i>Para</i>	1,2,4-tri	74.5	-12.2
1,2,3-tri	1,2,3,4-tetra	52.1	-19.3
1,2,3-tri	1,2,3,5-tetra	76.1	-20.6
1,2,4-tri	1,2,3,4-tetra	62.6	-4.4
1,2,4-tri	1,2,3,5-tetra	69.4	-6.1
1,2,4-tri	1,2,4,5-tetra	62.9	-20.7
1,3,5-tri	1,2,3,5-tetra	55.3	-26.9
1,2,3,4-tetra	Penta	61.5	-18.0
1,2,3,5-tetra	Penta	56.1	-8.6
1,2,4,5-tetra	Penta	37.5	-14.7
penta	Hexa	87.6	-12.7

<sup>a</sup> $\Delta H_{act}$  values are reported at 473 K

**Table S5.** Activation enthalpies and energies of concerted methylation.

Reactants	Products	Methylation Agent			
		CH <sub>3</sub> OH		CH <sub>3</sub> OCH <sub>3</sub>	
		$\Delta H_{act}^a$ kJ mol <sup>-1</sup>	$\Delta S_{act}$ J mol <sup>-1</sup> K <sup>-1</sup>	$\Delta H_{act}^a$ kJ mol <sup>-1</sup>	$\Delta S_{act}$ J mol <sup>-1</sup> K <sup>-1</sup>
Benzene	Toluene	119.9	-20.0	120.0	-8.4
Toluene	<i>Ortho</i>	127.2	-20.9	118.6	-1.0
Toluene	<i>Meta</i>	133.7	-17.7	121.7	-14.4
Toluene	<i>Para</i>	130.0	-16.5	102.5	-9.7
<i>Ortho</i>	1,2,3-tri	131.7	-12.9	126.7	7.4
<i>Ortho</i>	1,2,4-tri	122.8	-18.7	125.5	-3.2
<i>Meta</i>	1,3,5-tri	112.7	-19.7	122.5	-5.6
<i>Meta</i>	1,2,3-tri	130.0	-25.1	119.5	-11.6
<i>Meta</i>	1,2,4-tri	121.7	-18.0	120.9	5.3
<i>Para</i>	1,2,4-tri	108.9	-21.2	126.2	19.2
1,2,3-tri	1,2,3,4-tetra	136.7	-11.9	143.9	-7.1
1,2,3-tri	1,2,3,5-tetra	140.5	-7.6	151.6	-2.2
1,2,4-tri	1,2,3,4-tetra	118.8	1.5	118.5	-16.3
1,2,4-tri	1,2,3,5-tetra	126.8	3.7	133.9	-4.0
1,2,4-tri	1,2,4,5-tetra	138.8	-3.5	140.2	-10.9
1,3,5-tri	1,2,3,5-tetra	109.9	-24.0	102.3	-10.7
1,2,3,4-tetra	Penta	139.3	-29.6	165.7	2.4
1,2,3,5-tetra	Penta	146.8	0.1	119.6	-22.0
1,2,4,5-tetra	Penta	116.5	-19.2	142.0	5.9
Penta	Hexa	83.5	-9.6	101.1	-28.1

<sup>a</sup> $\Delta H_{act}$  values are reported at 473 K

### S5. Details of Thermochemical Properties of Frequency Calculations

Frequency calculations were performed on all optimization and Dimer calculations. Frequency calculations are normal mode analyses and are used to determine zero-point vibrational energy (ZPVE), vibrational enthalpy (H<sub>vib</sub>), and vibrational free energy (G<sub>vib</sub>) for adsorbed species to calculate enthalpy (H):

$$H = E_0 + \text{ZPVE} + H_{\text{vib}} \quad (\text{S56})$$

and free energies (G):

$$G = E_0 + \text{ZPVE} + G_{\text{vib}} \quad (\text{S57})$$

Translational and rotational enthalpies and free energies are also calculated for gas phase species to determine gas phase enthalpy:

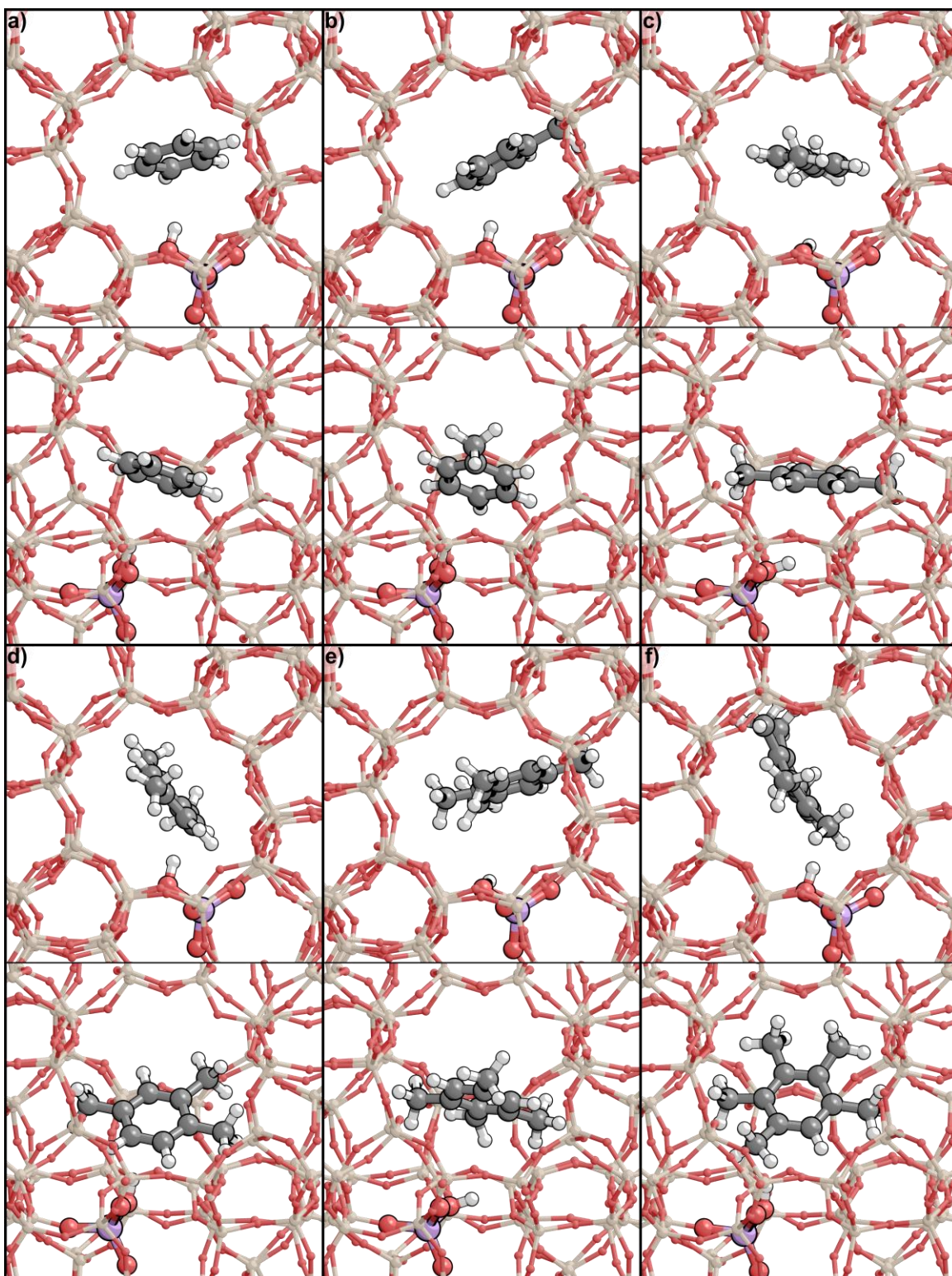
$$H = E_0 + \text{ZPVE} + H_{\text{vib}} + H_{\text{rot}} + H_{\text{trans}} \quad (\text{S58})$$

and gas phase free energies:

$$G = E_0 + \text{ZPVE} + G_{\text{vib}} + G_{\text{rot}} + G_{\text{trans}} \quad (\text{S59})$$

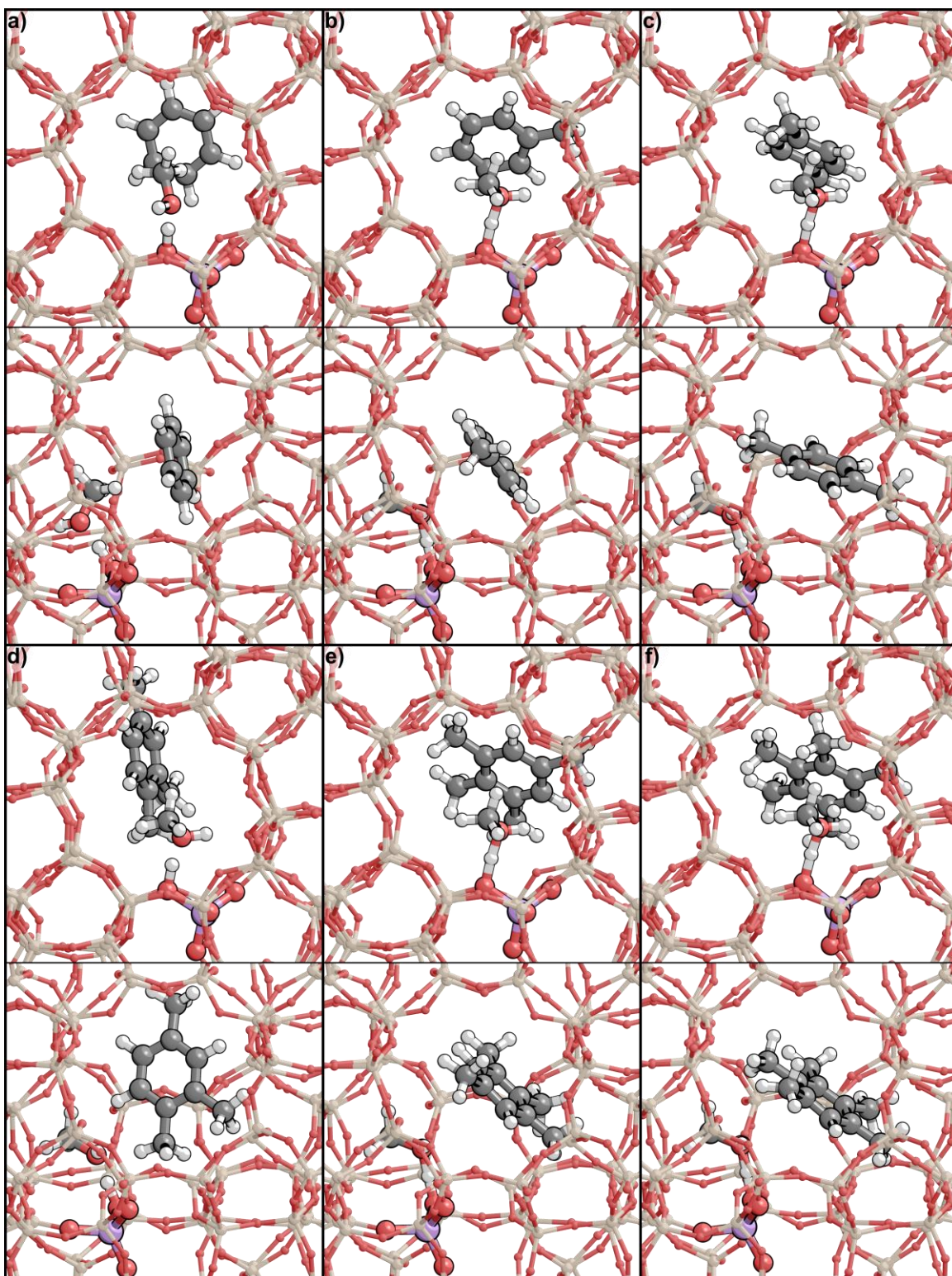
### S6. Most favorable orientations of reactant, product, and transition states



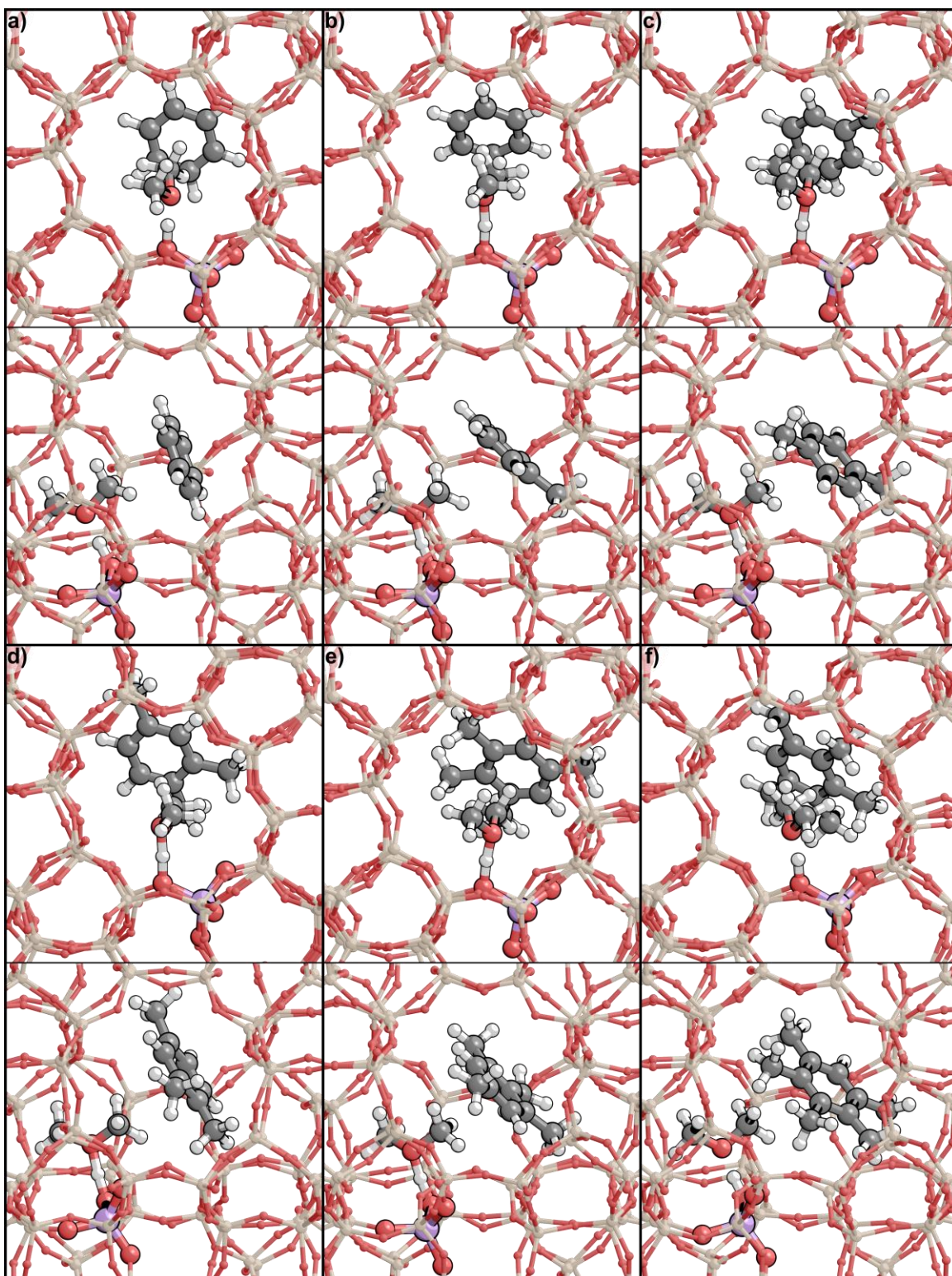


**Figure S22.** Most favorable orientations of a) benzene, b) toluene, c) *para*-xylene, d) 1,2,4-trimethylbenzene, e) 1,2,3,5-tetramethylbenzene, and f) pentamethylbenzene. Views are shown down the straight channel (top) and sinusoidal channel (bottom)



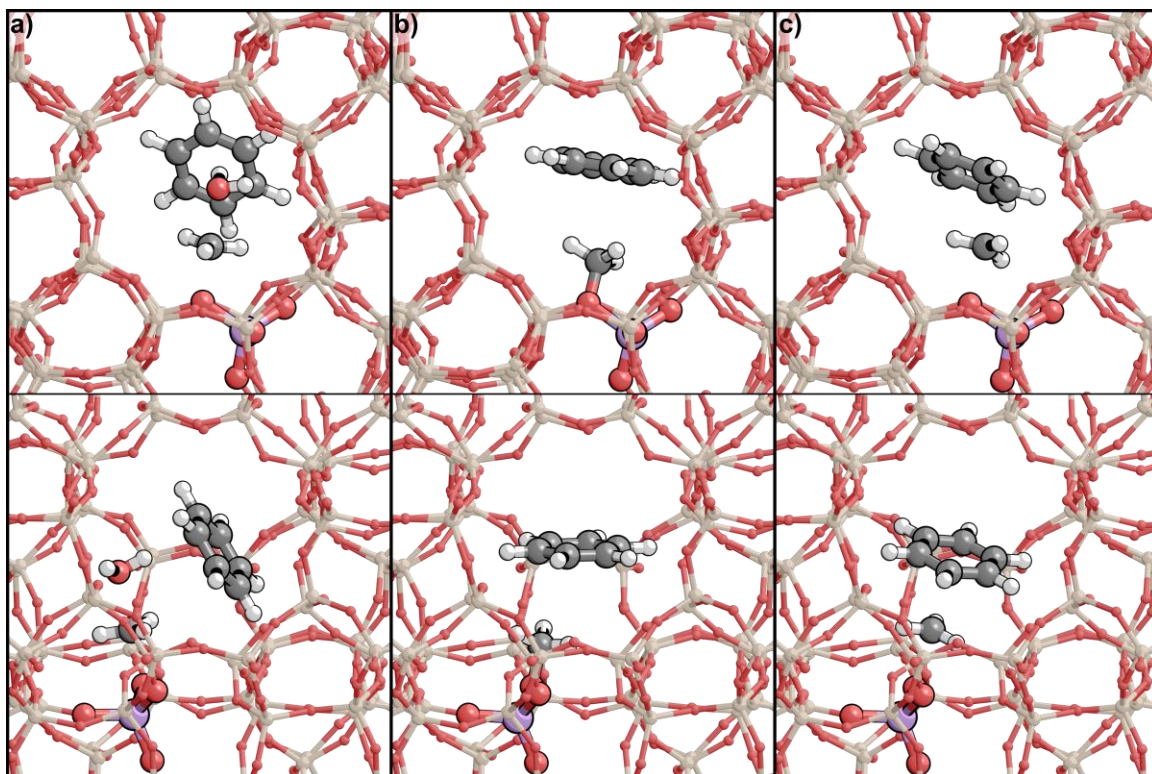


**Figure S23.** Most favorable orientation of  $\text{CH}_3\text{OH}$  co-adsorbed with a) benzene, b) toluene, c) *para*-xylene, d) 1,2,4-trimethylbenzene, e) 1,2,3,5-tetramethylbenzene, and f) pentamethylbenzene. Views are shown down the straight (top) and sinusoidal (bottom) channels of MFI.

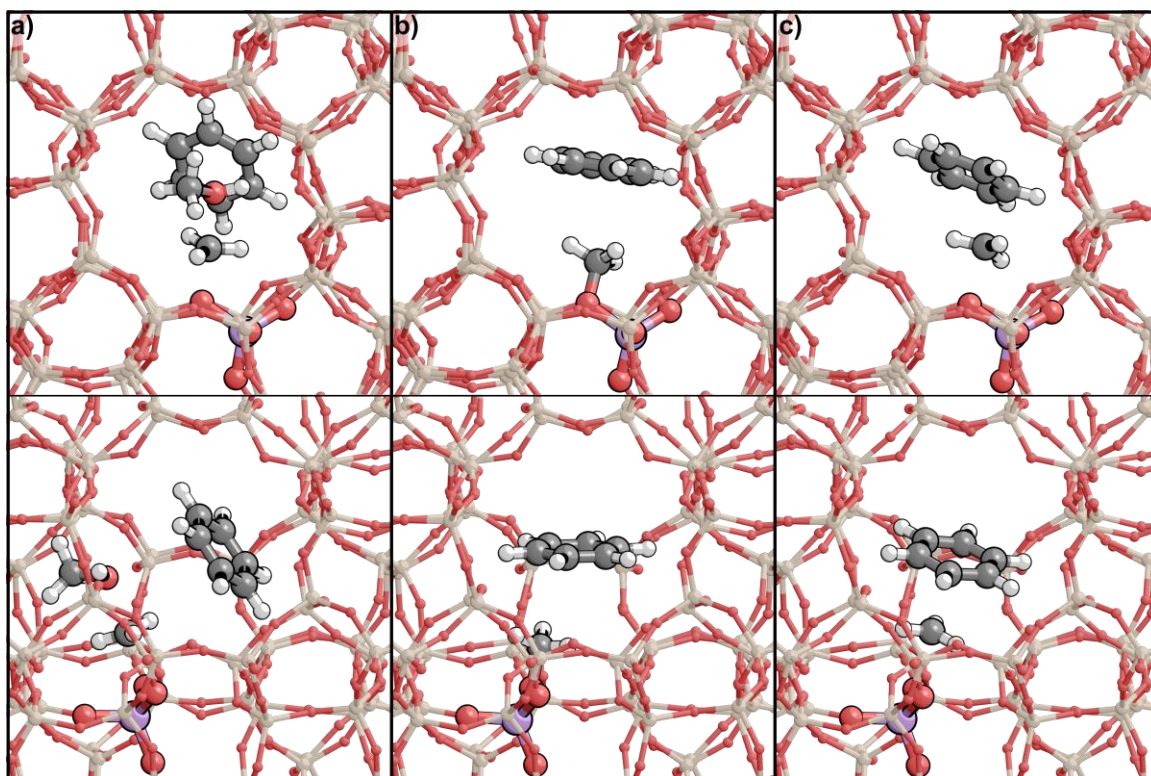


**Figure S24.** Most favorable orientation of  $\text{CH}_3\text{OCH}_3$  co-adsorbed with a) benzene, b) toluene, c) *para*-xylene, d) 1,2,4-trimethylbenzene, e) 1,2,3,5-tetramethylbenzene, and f) pentamethylbenzene. Views are shown down the straight (top) and sinusoidal (bottom) channels of MFI.

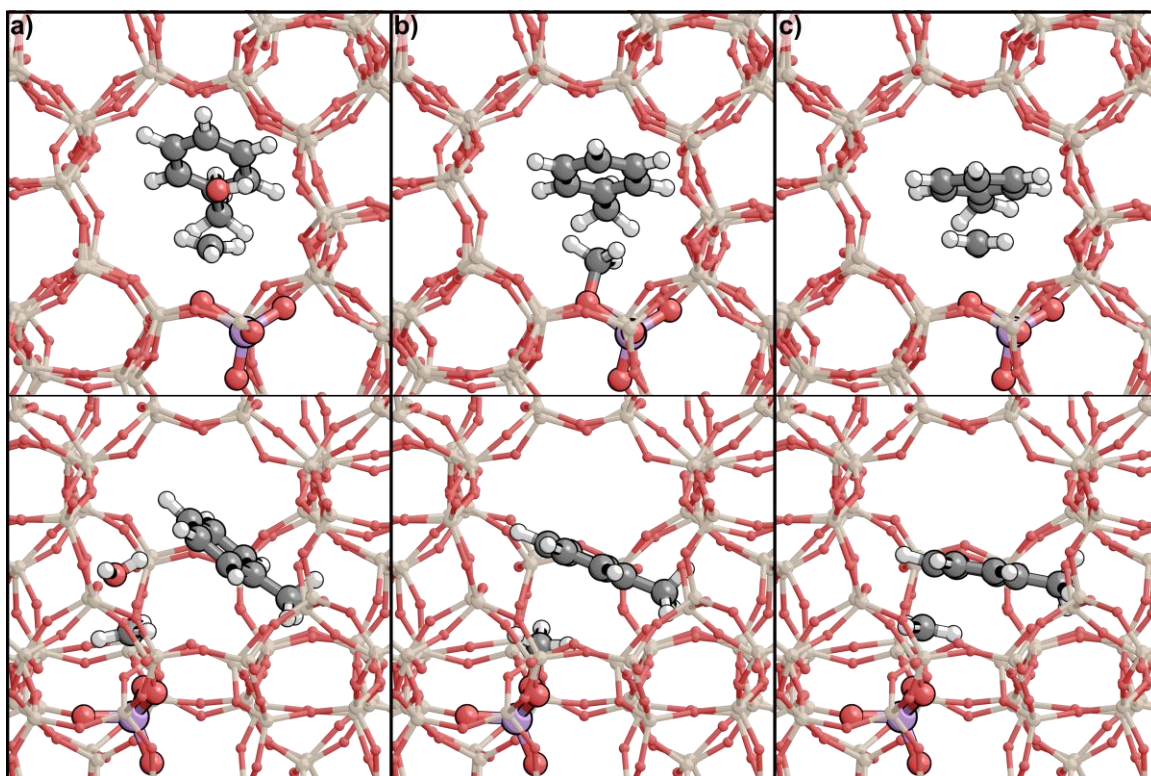




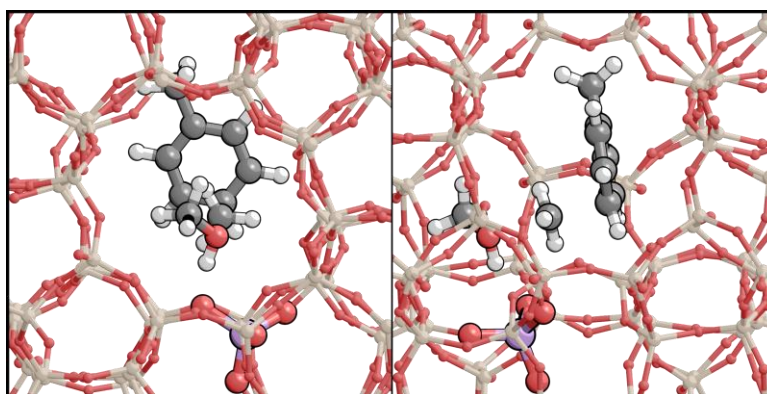
**Figure S25.** A) Surface methylation, b)  $\text{CH}_3\text{-Z-C}_6\text{H}_6$ , and c) ring methylation states of sequential methylation of benzene to toluene by  $\text{CH}_3\text{OH}$ . Views are shown down the straight (top) and sinusoidal (bottom) channels.



**Figure S26.** A) Surface methylation, b)  $\text{CH}_3\text{-Z-C}_6\text{H}_6$ , and c) ring methylation states of sequential methylation of benzene to toluene by  $\text{CH}_3\text{OCH}_3$ . Views are shown down the straight (top) and sinusoidal (bottom) channels.

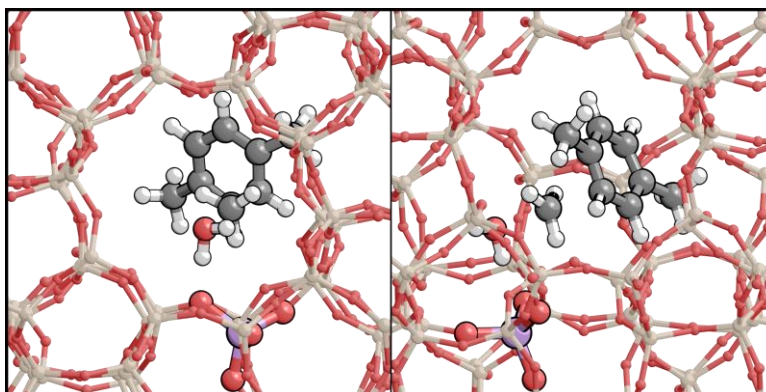


**Figure S27.** A) Surface methylation, b)  $\text{CH}_3\text{-Z-C}_7\text{H}_8$ , and c) ring methylation states of sequential methylation of toluene to *para*-xylene by  $\text{CH}_3\text{OH}$ . Views are shown down the straight (top) and sinusoidal (bottom) channels.

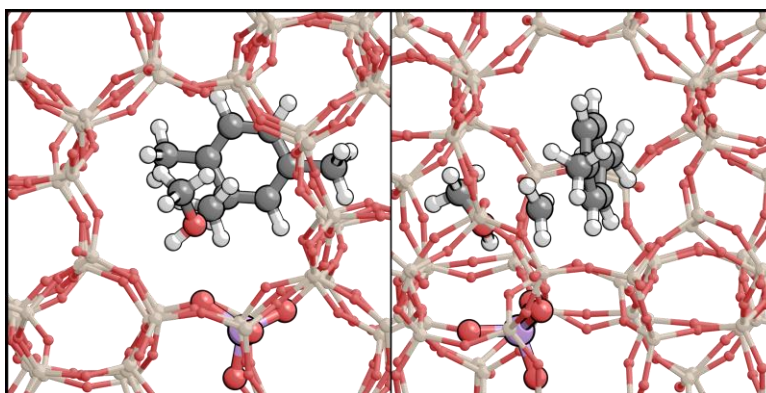


**Figure S28.** Concerted methylation transition state of toluene into *para*-xylene with  $\text{CH}_3\text{OCH}_3$ . Views are shown down the straight (left) and sinusoidal (right) channels.

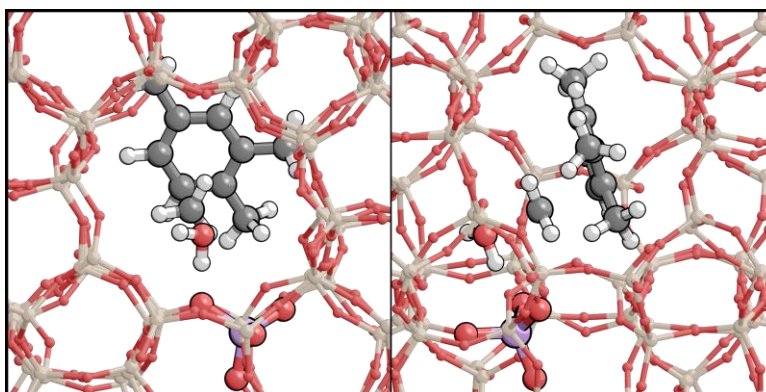




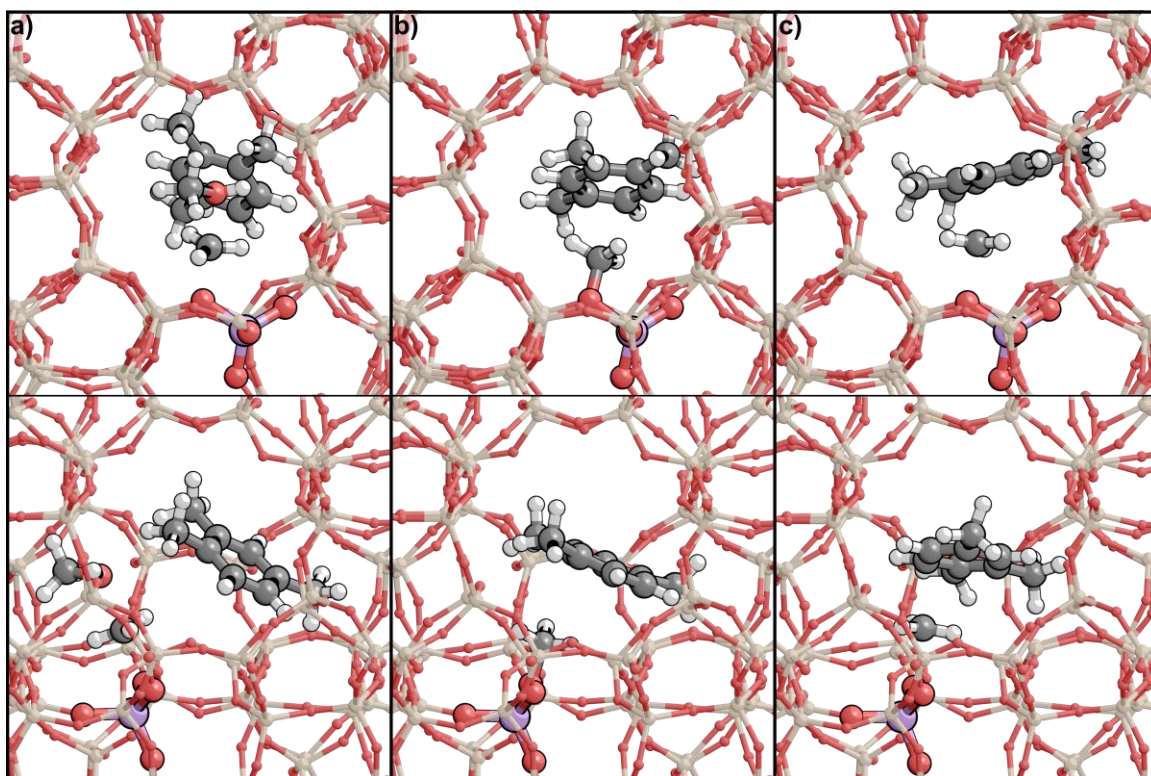
**Figure S29.** Concerted methylation transition state of *para*-xylene to 1,2,4-trimethylbenzene with  $\text{CH}_3\text{OH}$ . Views are shown down the straight (left) and sinusoidal (right) channels.



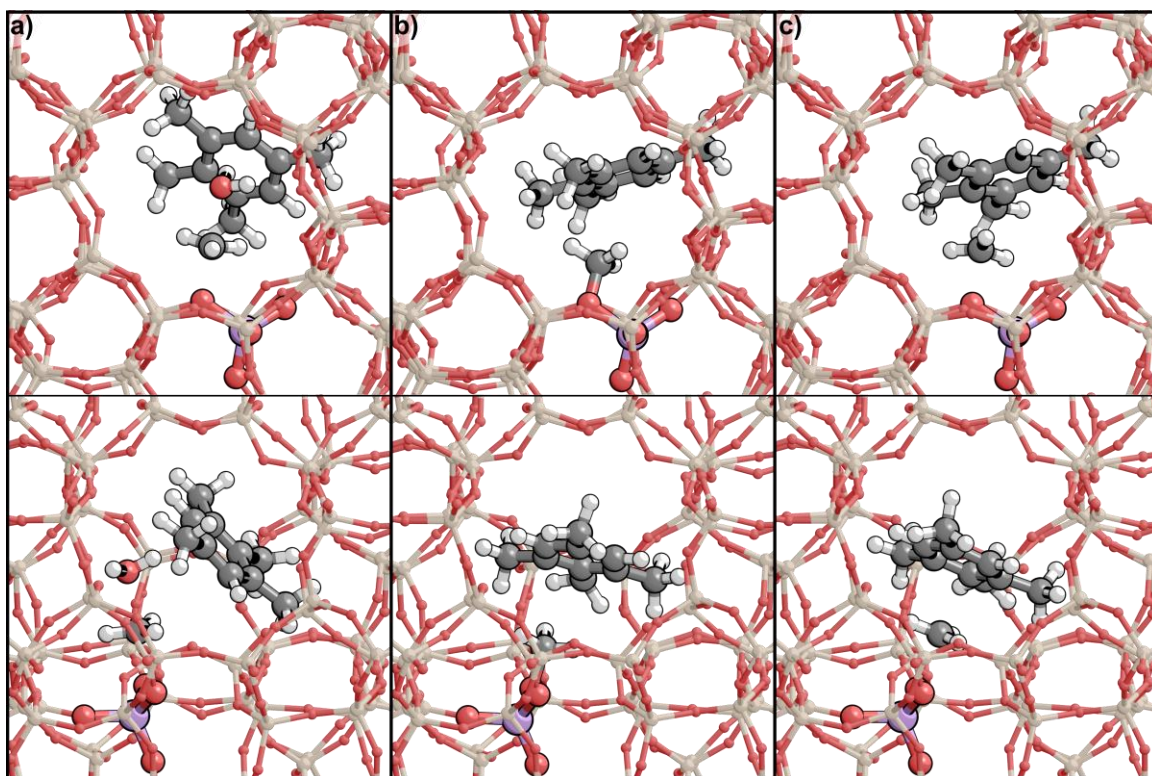
**Figure S30.** Concerted methylation transition state of *para*-xylene to 1,2,4-trimethylbenzene with  $\text{CH}_3\text{OCH}_3$ . Views are shown down the straight (left) and sinusoidal (right) channels.



**Figure S31.** Concerted methylation transition state of 1,2,4-trimethylbenzene to 1,2,3,5-tetramethylbenzene with  $\text{CH}_3\text{OH}$ . Views are shown down the straight (left) and sinusoidal (right) channels.

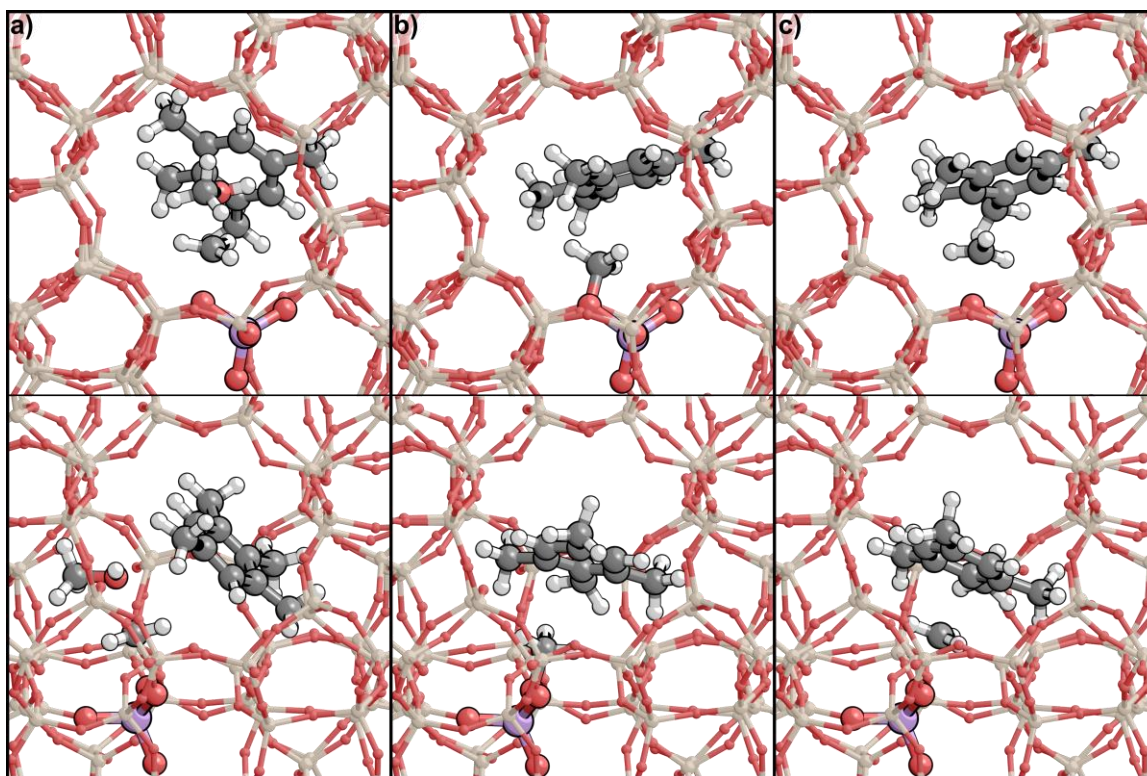


**Figure S32.** A) Surface methylation, b)  $\text{CH}_3\text{-Z--C}_9\text{H}_{11}$ , and c) ring methylation states of sequential methylation of 1,2,4-trimethylbenzene to 1,2,3,5-tetramethylbenzene by  $\text{CH}_3\text{OCH}_3$ . Views are shown down the straight (top) and sinusoidal (bottom) channels.

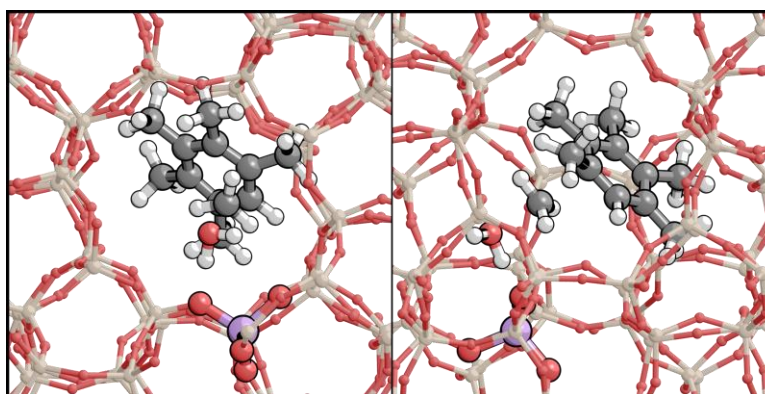


**Figure S33.** A) Surface methylation, b)  $\text{CH}_3\text{-Z--C}_{10}\text{H}_{14}$ , and c) ring methylation states of sequential methylation of 1,2,3,5-tetramethylbenzene to pentamethylbenzene by  $\text{CH}_3\text{OH}$ . Views are shown down the straight (top) and sinusoidal (bottom) channels.

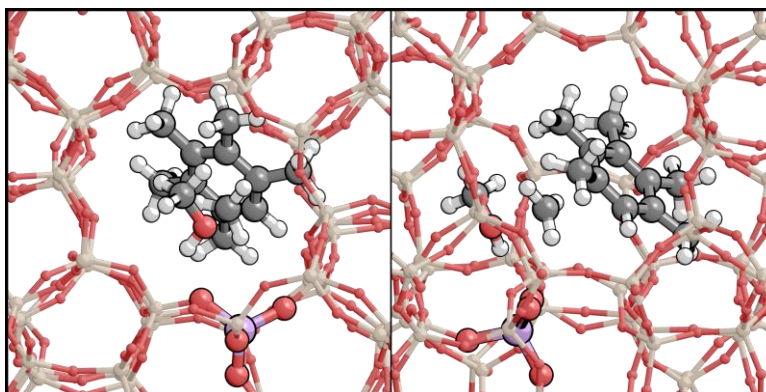




**Figure S34.** A) Surface methylation, b)  $\text{CH}_3\text{-Z--C}_{10}\text{H}_{14}$ , and c) ring methylation states of sequential methylation of 1,2,3,5-tetramethylbenzene to pentamethylbenzene by  $\text{CH}_3\text{OCH}_3$ . Views are shown down the straight (top) and sinusoidal (bottom) channels.



**Figure S35.** Concerted methylation transition state of pentamethylbenzene to hexamethylbenzene with  $\text{CH}_3\text{OH}$ . Views are shown down the straight (left) and sinusoidal (right) channels.



**Figure S36.** Concerted methylation transition state of pentamethylbenzene to hexamethylbenzene with  $\text{CH}_3\text{OCH}_3$ . Views are shown down the straight (left) and sinusoidal (right) channels.